

ΑΣΚΗΣΗ 1

$$F(x,y,z) = x'y' + yz + x'yz' = x'y'z + x'y'z' + xyz + x'yz + x'yz'$$

$\downarrow$   $x'y'(z+z')$        $\rightarrow$   $yz(x+x')$        $+x'yz'$

x	y	z	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	
1	0	1	
1	1	0	
1	1	1	1

x \ yz	00	01	11	10
0	1	1	1	1
1			1	

$\rightarrow x'$

$\swarrow$  yz

$$F = x' + yz$$

ΑΣΚΗΣΗ 2

$$F(x, y, z) = x'y + yz' + y'z' = x'y(z+z') + yz'(x+x') + y'z'(x+x') = x'yz + x'yz' + xyz' + x'yz' + xy'z' + x'y'z'$$

x	y	z	F
0	0	0	1
0	0	1	
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	
1	1	0	1
1	1	1	

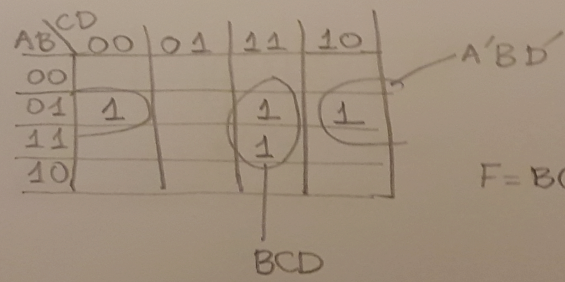
x	yz			
	00	01	11	10
0	1		1	1
1	1			1

$$F = z' + x'y$$

ΑΣΚΗΣΗ 3

$$F(A,B,C,D) = \Sigma(4,6,7,15)$$

	A	B	C	D	F
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	1
5	0	1	0	1	
6	0	1	1	0	1
7	0	1	1	1	1
8	1	0	0	0	
9	1	0	0	1	
10	1	0	1	0	
11	1	0	1	1	
12	1	1	0	0	
13	1	1	0	1	
14	1	1	1	0	
15	1	1	1	1	1



$$F = BCD + A'BD'$$

ΑΣΚΗΣΗ 4

	A	B	C	D	F
0	0	0	0	0	
1	0	0	0	1	1
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	1
5	0	1	0	1	1
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	1
10	1	0	1	0	1
11	1	0	1	1	1
12	1	1	0	0	
13	1	1	0	1	
14	1	1	1	0	
15	1	1	1	1	1

$$F = A'B'C'D + AB'D + A'BC' + ABCD + ABC =$$

$$ABC(D+D')$$

$$A'BC'(D+D')$$

apa  $F = A'B'C'D + A'BC'D +$   
 $+ A'BC'D + A'BC'D +$   
 $+ A'BC'D + ABCD +$   
 $+ ABCD + A'BC'D'$

AB \ CD	00	01	11	10
00		1		
01	1	1		
11			1	
10		1	1	1

$A'BC'$  (circled 1s at (00,01) and (01,01))  
 $ABC'$  (circled 1 at (11,11))  
 $B'C'D$  (circled 1s at (01,01) and (10,01))  
 $ACD$  (circled 1s at (10,11) and (10,10))

$$F = B'C'D + ACD + ABC' + A'BC'$$

## ΑΣΚΗΣΗ 5

Αποδοτίστε την συνάρτηση  $F$  και υλοποιήστε τη με κυκλώματα πυλών NAND 2 επιπέδων.

$$F = A'B'C'D + CD + AC'D$$

AB \ CD	00	01	11	10
00		1	1	
01			1	
11		1	1	
10		1	1	

$$F = AD + B'D + CD$$

AD

B'D

$$F = AD + B'D + CD = ((AD)' \cdot (B'D)' \cdot (CD)')'$$

διότι

$$\text{De Morgan} : (x+y)' = x'y'$$

$$F = (F')' \Rightarrow \dots$$

Άρα

