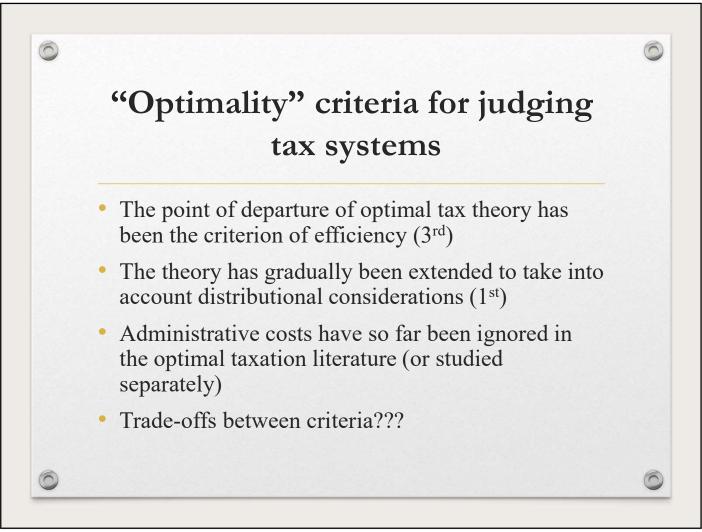
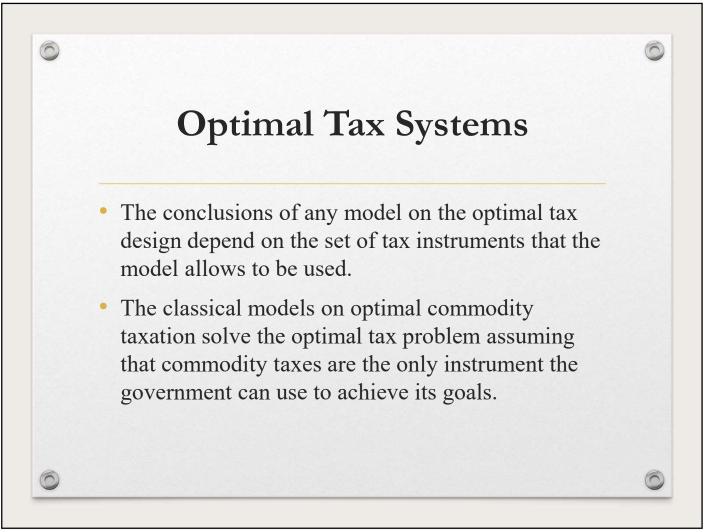
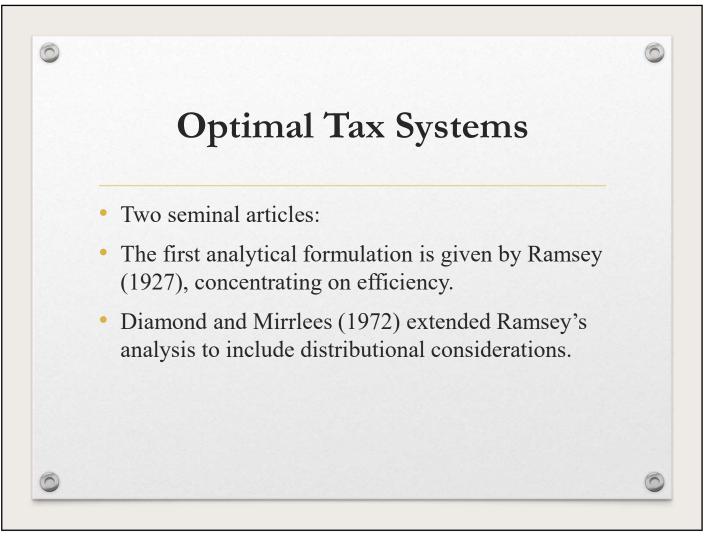


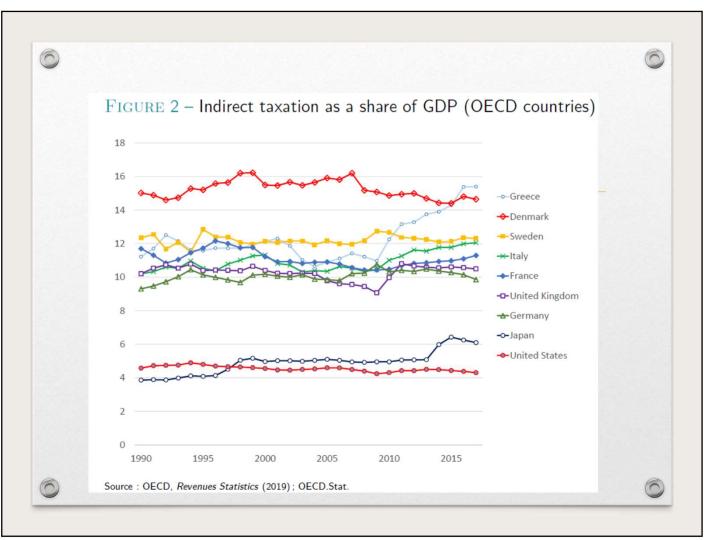
- to different people)
- A good tax system is one which minimizes the resource cost involved in assessing, collecting and paying the taxes (administrative and compliance cost)
- A good tax system minimizes the efficiency cost of taxation, in terms of the distortions they cause in agents' behaviour

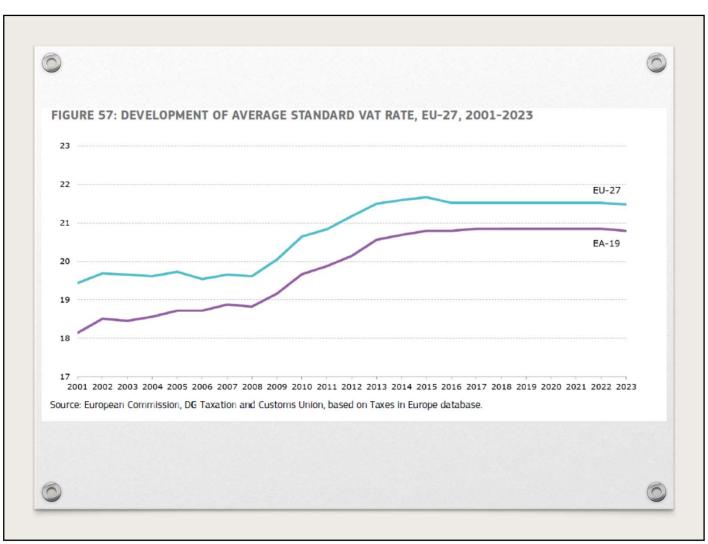


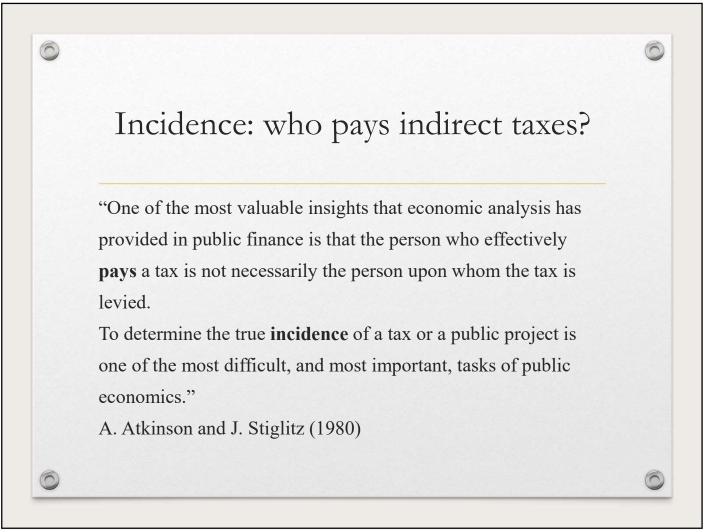
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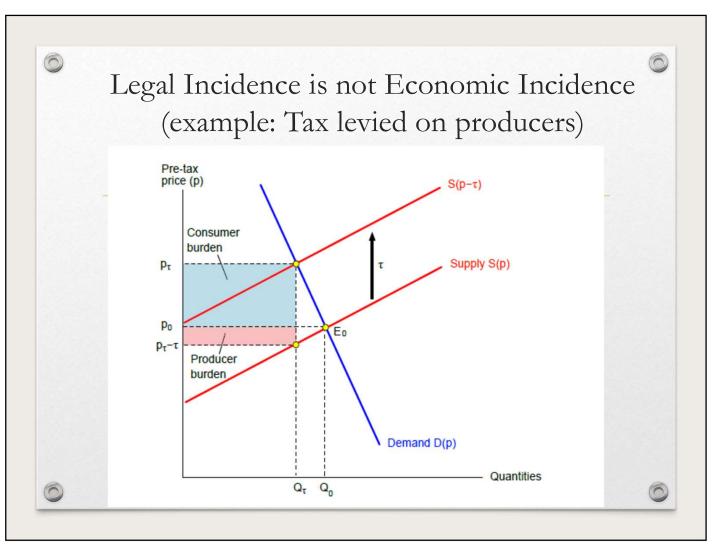


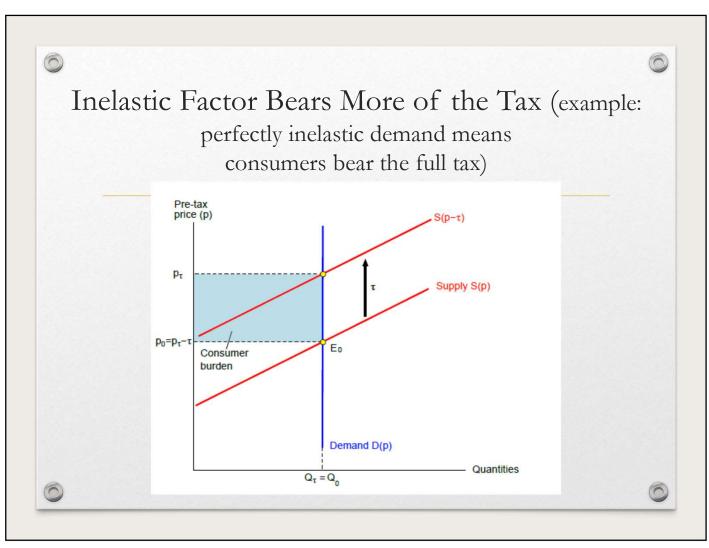


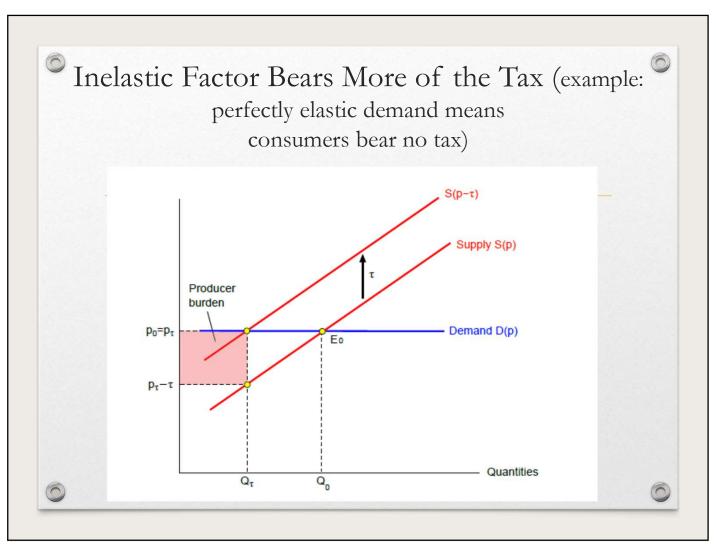


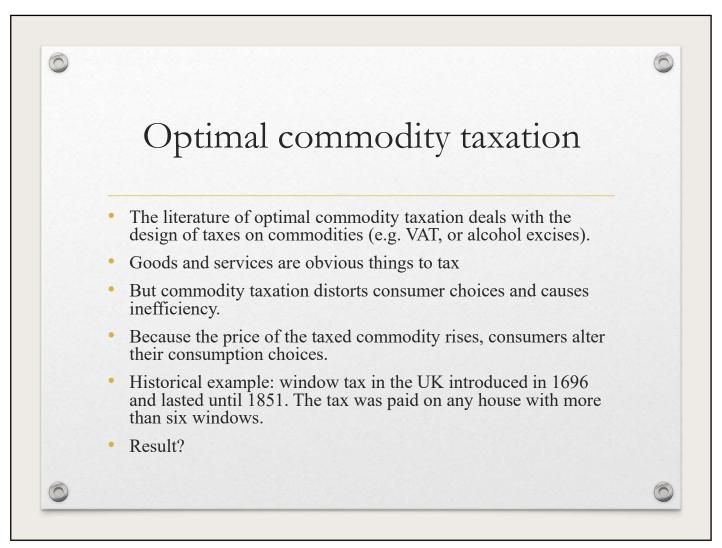


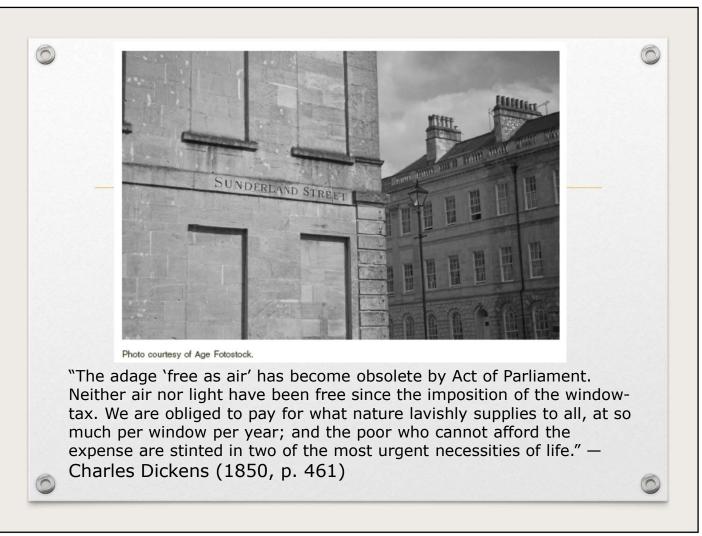
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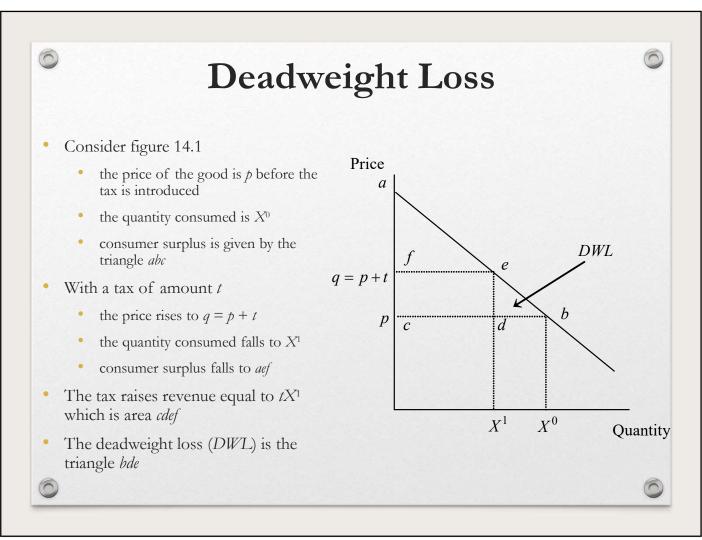


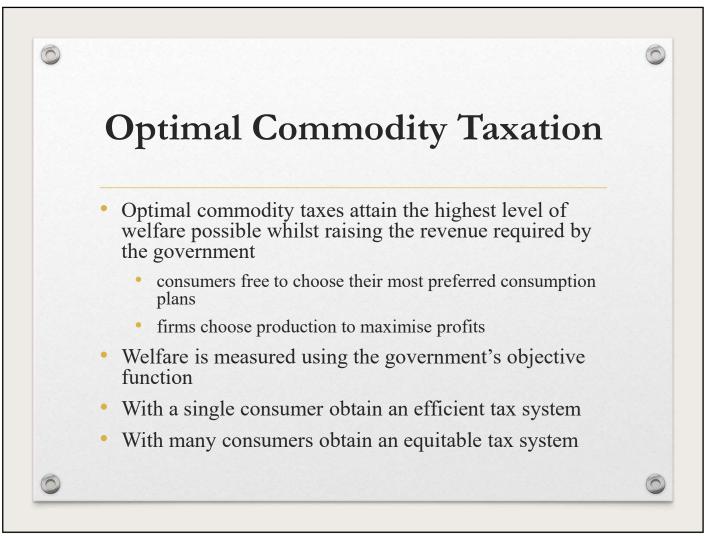








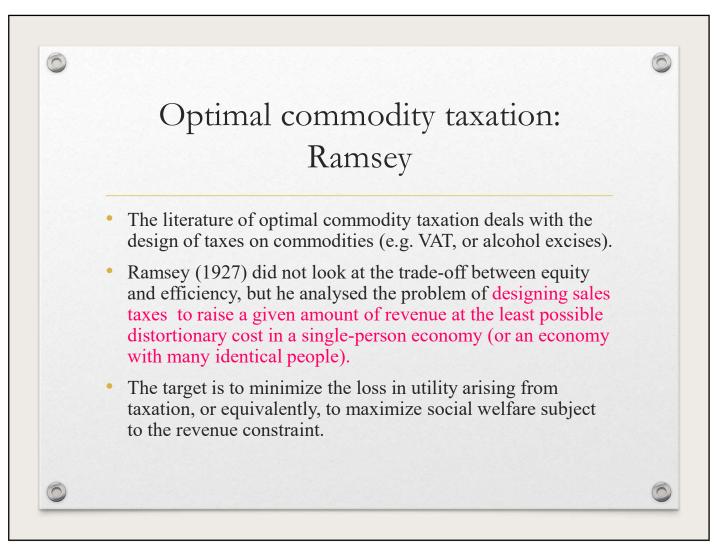


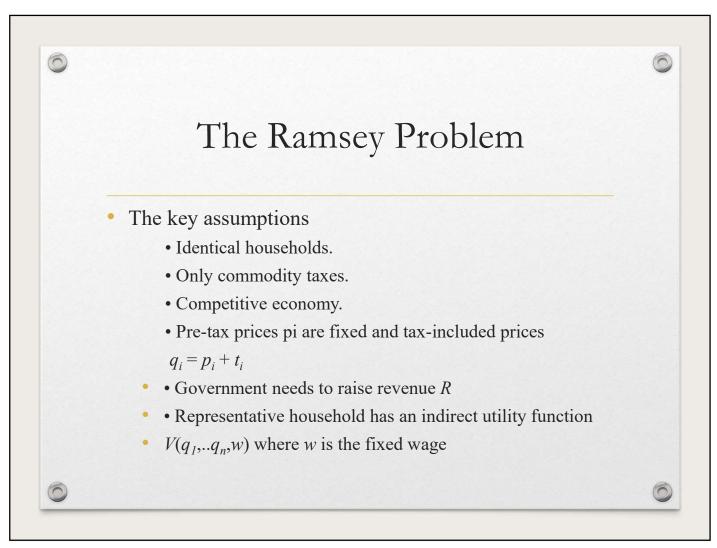


## The Ramsey problem

- Problem set by Pigou to his 24 year-old student
- "A given revenue is to be raised by proportionate taxes on some or all uses of income, the taxes on different uses being possibly at different rates; how should these rates be adjusted in order that the decrement of utility may be a minimum?
- I propose to neglect altogether questions of distribution and considerations arising from the differences in the marginal utility of money to different people; and I shall deal only with a purely competitive system with no foreign trade."

  Ramsey (1927)







## Optimal commodity taxation: Ramsey



- Suppose that there *n* commodities in the economy and a single form of labour, *l*.
- Producer prices are **p** and the wage rate faced by the consumer is w.
- The consumer faces consumer prices  $\mathbf{q}$  and has a budget constraint  $\mathbf{q}\mathbf{x} = wl$ .
- The government must raise a given amount of revenue,  $\it R$  by imposing unit taxes

$$\mathbf{t} = (t_1, t_2, ..., t_n).$$

where  $t_k$  is the difference between consumer price  $(q_k)$  and producer price  $(p_k)$ . Assume producer prices to be fixed (constant returns to scale). Selecting tax structure  $\equiv$  choosing a structure for consumer prices.

• The preferences of the representative consumer are represented by the indirect utility function V, defined over prices,  $U = V(\mathbf{q}, w)$ .





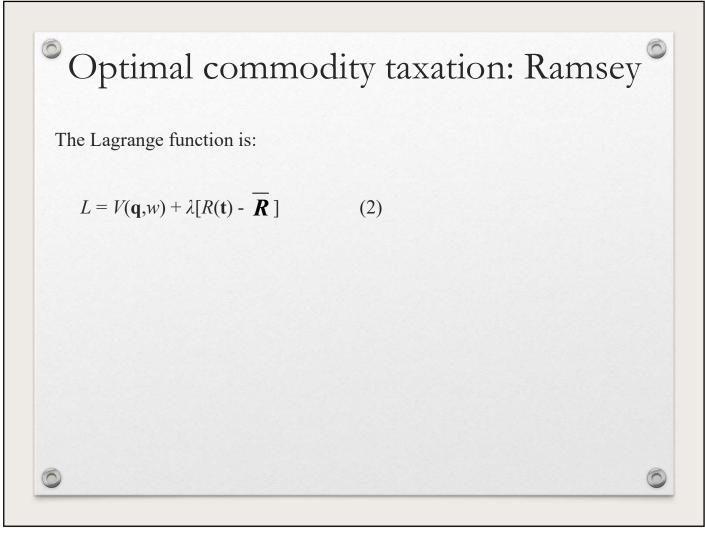


Our problem then is to choose  $t_i$ s so as to maximise consumer utility subject to the revenue constraint of the government, that is

Maximise 
$$V(\mathbf{q}, w)$$
, subject to  $R(\mathbf{t}) = \sum_{k} t_{k} x_{k} \ge \overline{R}$  (1)

where  $x_k$  is the consumption of the kth good by the consumer.

0

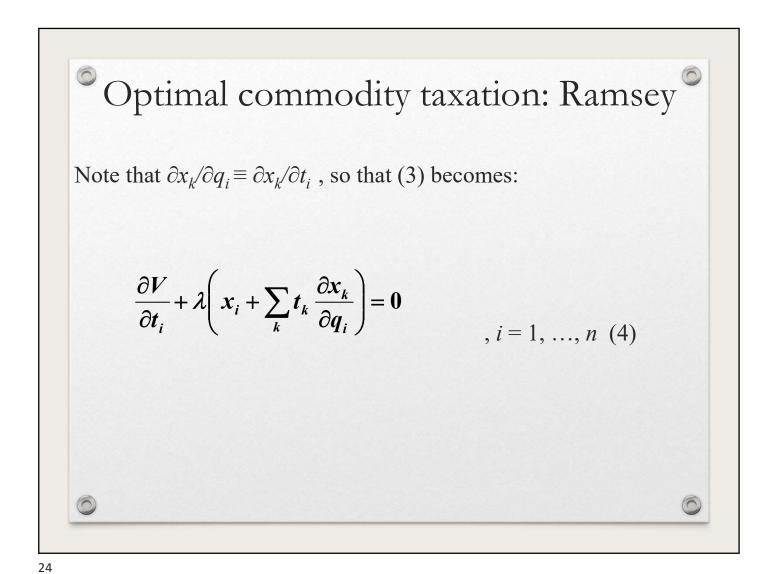




• Set the partial derivatives of L with respect to the tax rates equal to zero:

$$\frac{\partial L}{\partial t_i} = \frac{\partial V}{\partial t_i} + \lambda \frac{\partial R(t)}{\partial t_i} = 0$$

$$, i = 1, ..., n (3)$$



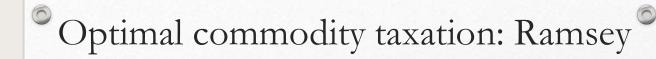


• Using duality in consumer theory, Roy's identity gives:

$$\frac{\partial V}{\partial q_i} = -x_i \frac{\partial V}{\partial M} = -ax_i \tag{5}$$

where a is the marginal utility of income (M).





• The Slutsky equation decomposes the change in demand due to a price change  $(\partial x_k/\partial q_i)$  into an income and a symmetric substitution effect):

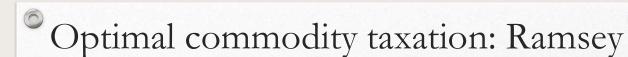
$$\frac{\partial \mathbf{x}_{k}}{\partial \mathbf{q}_{i}} = -\mathbf{x}_{i} \frac{\partial \mathbf{x}_{k}}{\partial \mathbf{M}} + \mathbf{s}_{ki} \qquad i, k = 1, ..., n \tag{6}$$

Where M is income and  $s_{ki}$  is the substitution effect  $\left(\left(\frac{\partial x_k}{\partial q_i}\right)_{U_i}\right)$ 

or the utility-compensated change in demand for the *k*th good when the price of the *i*th good changes.







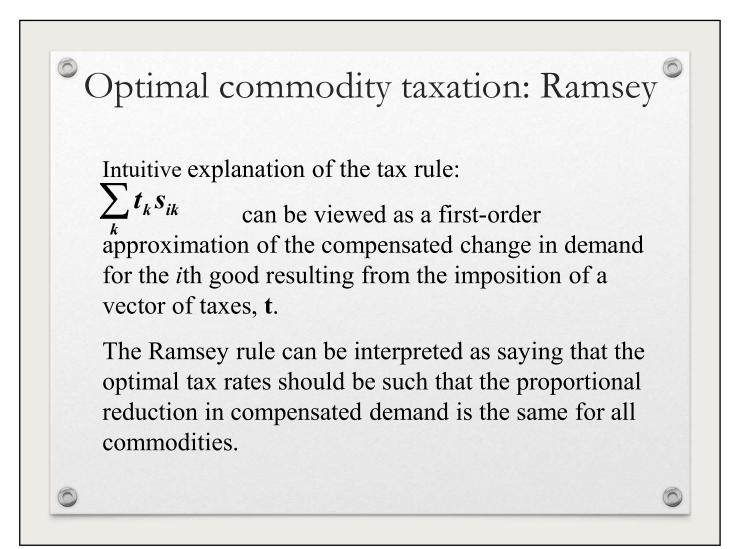
• Substituting (5) and (6) into (4) and after rearranging and utilizing the fact that the substitution effects are symmetric  $(s_{ik} = s_{ki})$ ,:

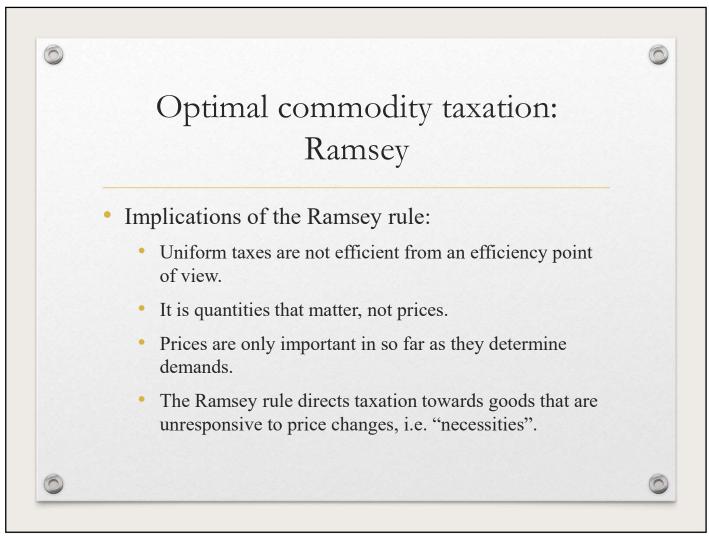
$$\frac{\left(\sum_{k} t_{k} s_{ik}\right)}{x_{i}} = -9, \quad \text{where} \quad \theta = 1 - \frac{\alpha}{\lambda} - \sum_{k} t_{k} \frac{\partial x_{k}}{\partial M} \tag{7}$$

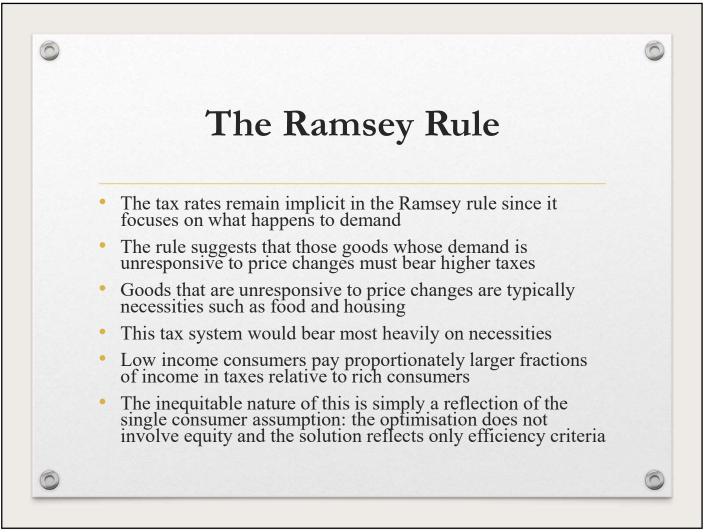
This is the Ramsey tax rule. Notice that g is a positive number independent of i.

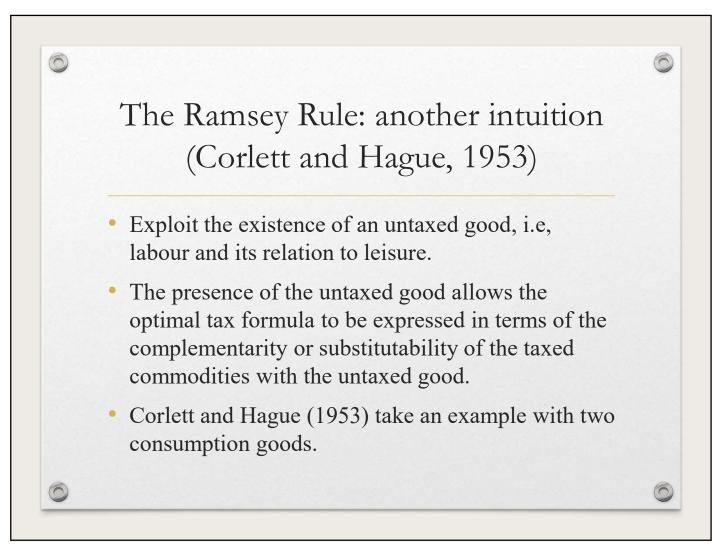


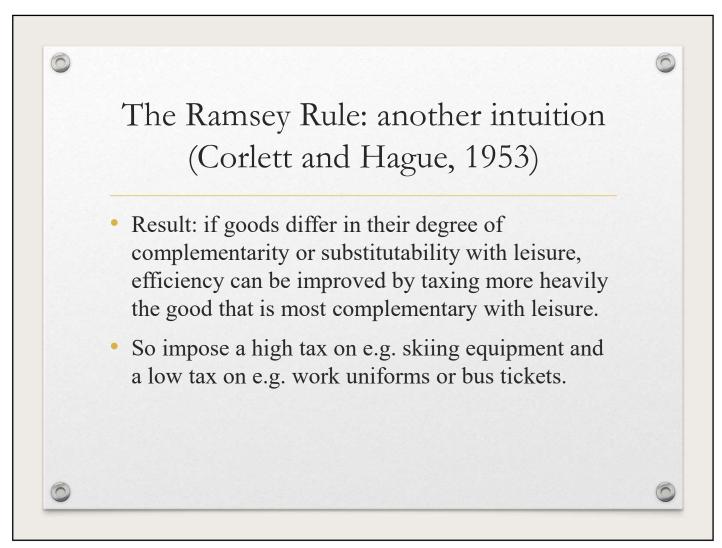














## Inverse elasticity rule

- The general intuition behind the Ramsey rule is clear, but there is no explicit formula for the calculation of taxes.
- More precise tax rules can be achieved at the expense of additional assumptions.
- Assume all cross-price effects to be zero.
- Take equation (4) as the starting point:

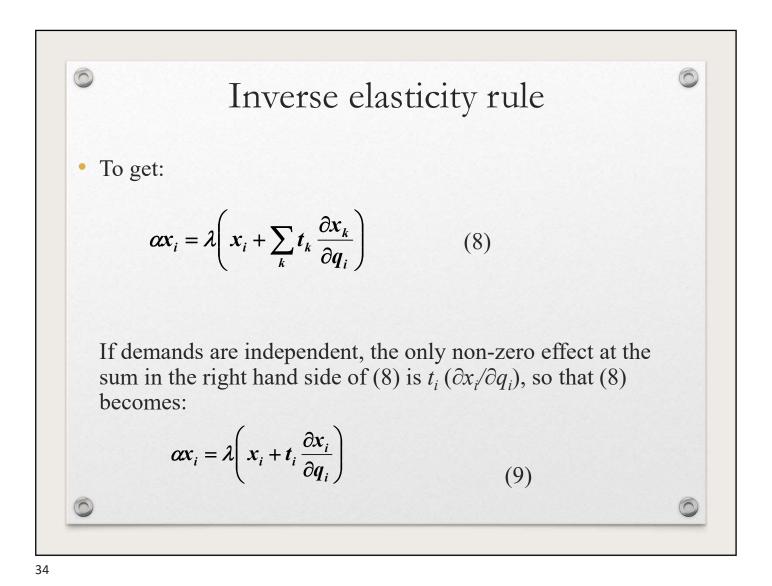
$$\frac{\partial V}{\partial t_i} + \lambda \left( x_i + \sum_k t_k \frac{\partial x_k}{\partial q_i} \right) = 0$$

And replace Roy's identity

$$\frac{\partial V}{\partial q_i} = -x_i \frac{\partial V}{\partial M} = -ax_i$$

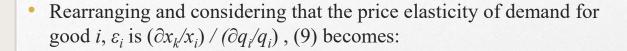








## Inverse elasticity rule



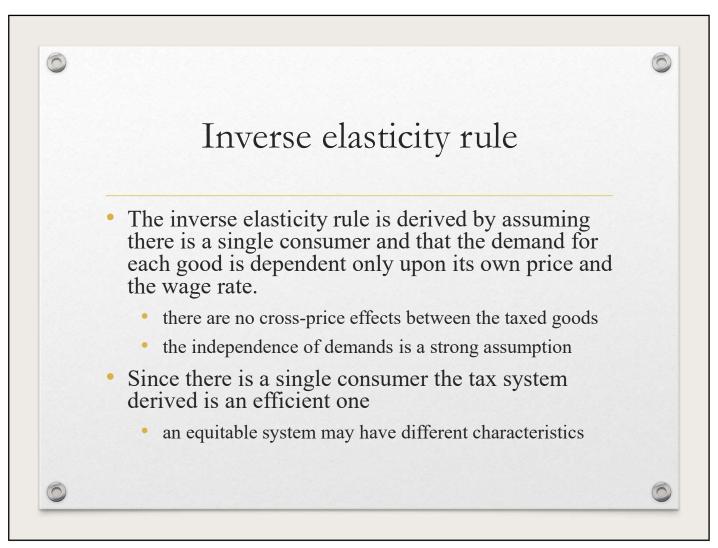
$$\frac{t_i}{p_i + t_i} = \left(\frac{\alpha - \lambda}{\lambda}\right) \frac{1}{\varepsilon_i}$$

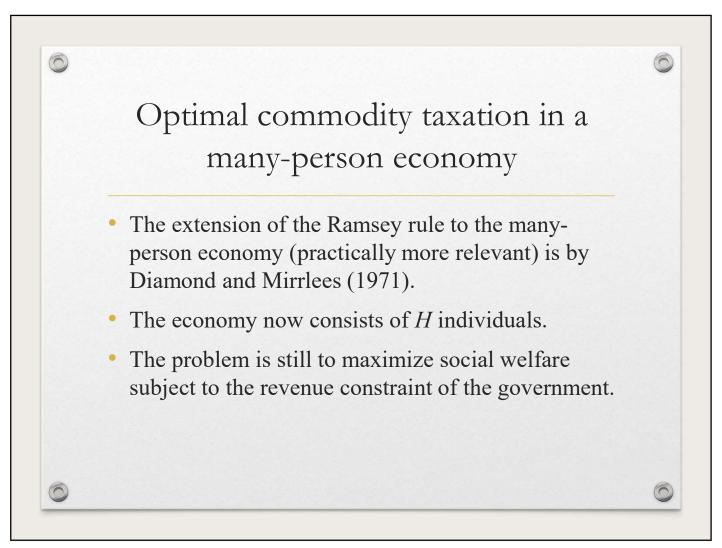
This is the well known inverse elasticities rule, which states that at the optimum, proportional rates of taxes should be inversely related to the price elasticity of demand of the good on which they are levied.

- These observations imply that necessities, which by definition have low elasticities of demand, should be highly taxed
- Luxuries with a high elasticity of demand should have a low rate of tax









## Optimal commodity taxation in a many-person economy

- Suppose that there are n commodities in the economy and a single form of labour, l.
- Producer prices are **p** and the wage rate faced by the consumer is w.
- The consumer faces consumer prices  $\mathbf{q}$  and has a budget constraint  $\mathbf{q}\mathbf{x} = w^h l$ .
- The government must raise a given amount of revenue,  $\overline{R}$  by imposing unit taxes

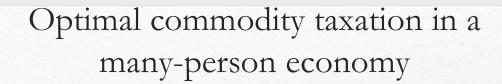
$$\mathbf{t} = (t_1, t_2, ..., t_n).$$

where  $t_k$  is the difference between consumer price  $(q_k)$  and producer price  $(p_k)$ . Assume producer prices to be fixed (constant returns to scale). Selecting tax structure  $\equiv$  choosing a structure for consumer prices.

• Individual welfare is determined in terms of the indirect utility function  $V^h$ , defined over prices,  $U^h = V^h(\mathbf{q}, w^h)$ .







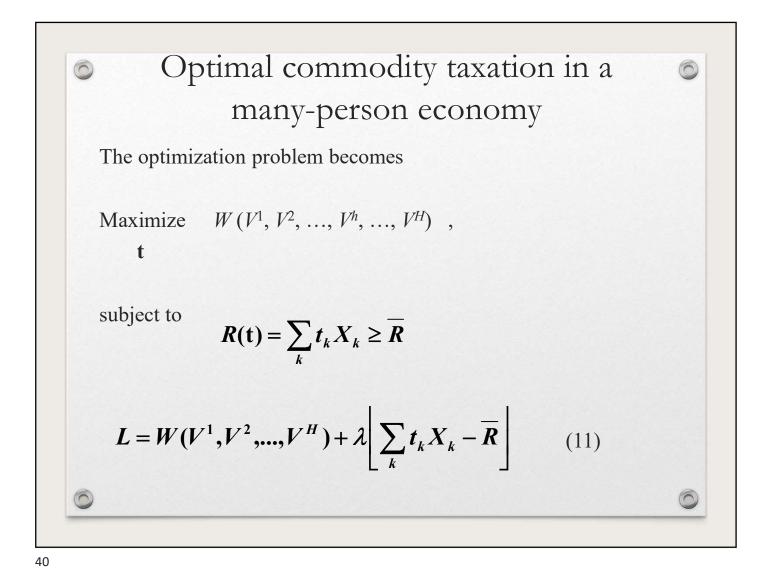
Social welfare is determined by a Bergson-Samuelson social welfare function, defined over individual utilities:

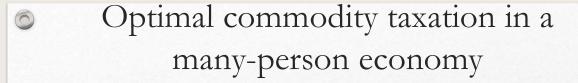
$$W = W(V^1, V^2, ..., V^h, ..., V^H)$$
 (10)

Total demand for commodity i is expressed as

$$X_i = \sum_h x_i^h$$

0

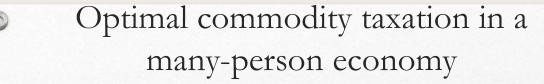




• Set the partial derivatives of L with respect to the tax rates equal to zero:

$$\frac{\partial L}{\partial q_i} = \sum_{h} \frac{\partial W}{\partial V^h} \frac{\partial V}{\partial q_i} + \lambda \left( X_i + \sum_{k} t_k \frac{\partial X_k}{\partial q_i} \right) = 0$$
 (12)

0



• Using duality in consumer theory, Roy's identity gives:

$$\frac{\partial V^h}{\partial q_i} = -x_i \frac{\partial V^h}{\partial M^h} = -a^h x_i$$

where  $a^h$  is the marginal utility of income  $(M^h)$  of individual h, we have:

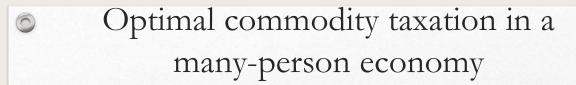
$$\sum_{h} \frac{\partial W}{\partial V^{h}} \frac{\partial V^{h}}{\partial q_{i}} = -\sum_{h} \frac{\partial W}{\partial V^{h}} \alpha^{h} x_{i}^{h}$$
(13)

Optimal commodity taxation in a many-person economy

Define

$$\beta^{h} = \frac{\partial W}{\partial V^{h}} \frac{\partial V^{h}}{\partial M} = \frac{\partial W}{\partial V^{h}} \alpha^{h}$$
(14)

 $\beta^h$  is very important and can be interpreted as the **social** marginal utility of income for individual h, that is the increase in social welfare resulting from a marginal increase in the income accruing to individual h.



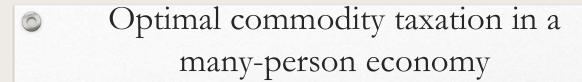
• Replacing (13) and (14) into (12) we get:

$$\sum_{h} \beta^{h} x_{i}^{h} = \lambda \left( X_{i} + \sum_{k} t_{k} \frac{\partial X_{k}}{\partial q_{i}} \right)$$
 (15)

• Substituting from the Slutsky equation as before, and after some algebraic manipulations (15) becomes:



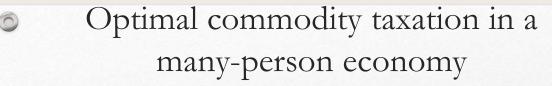




$$\frac{\sum_{h}\sum_{k}t_{k}s_{ik}^{h}}{X_{i}} = -\left[1 - \sum_{h}\frac{b^{h}}{H}\frac{x_{i}^{h}}{x_{i}}\right]$$

where 
$$b^h = \frac{\beta^h}{\lambda} + \sum_k t_k \frac{\partial x_k^h}{\partial M^h}$$

Remember that  $\beta^h$  is the **social marginal utility of income** for individual h.

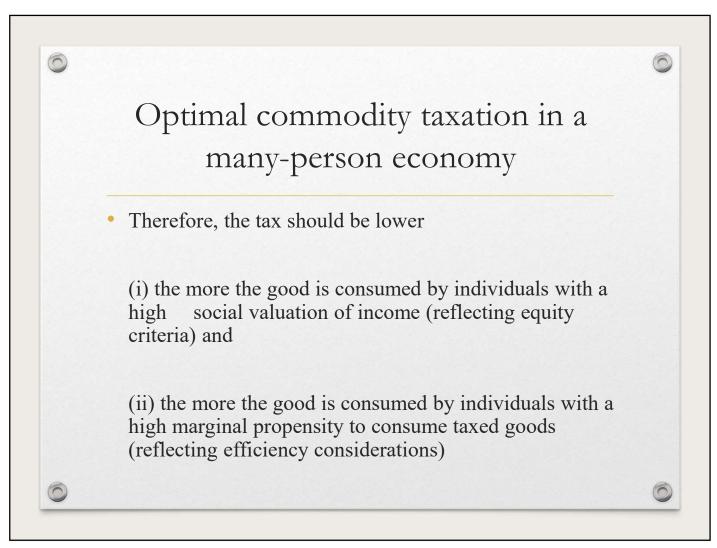


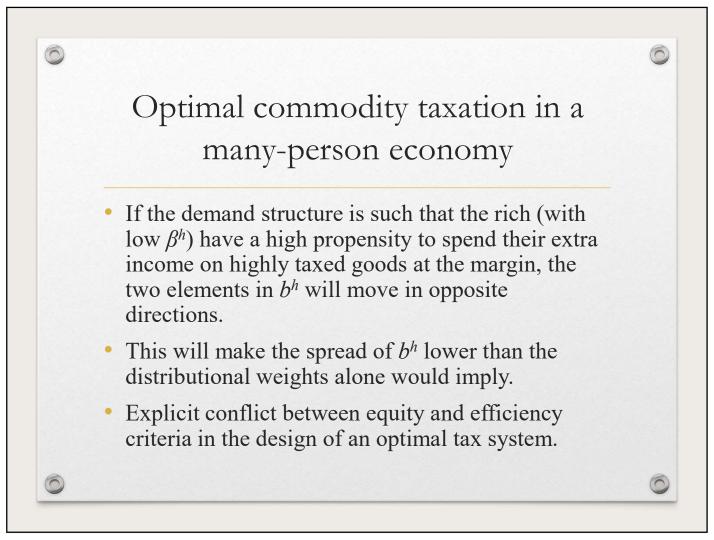
$$b^{h} = \frac{\beta^{h}}{\lambda} + \sum_{k} t_{k} \frac{\partial x_{k}^{h}}{\partial M^{h}}$$

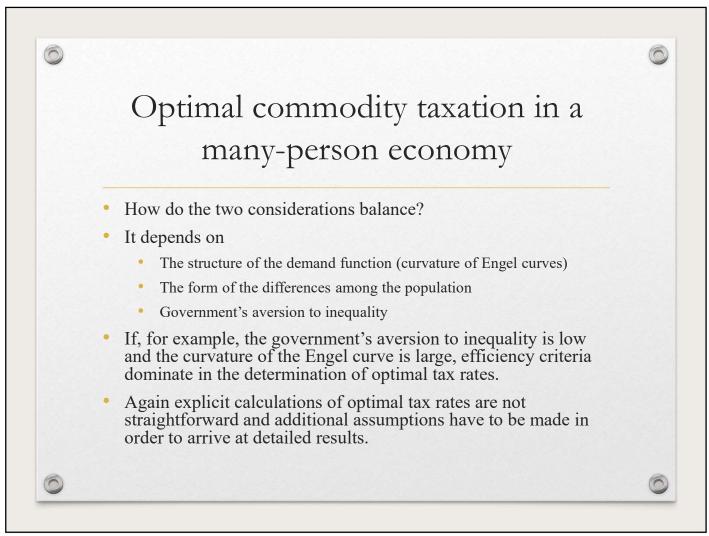
 $b^h$  consists of two elements,

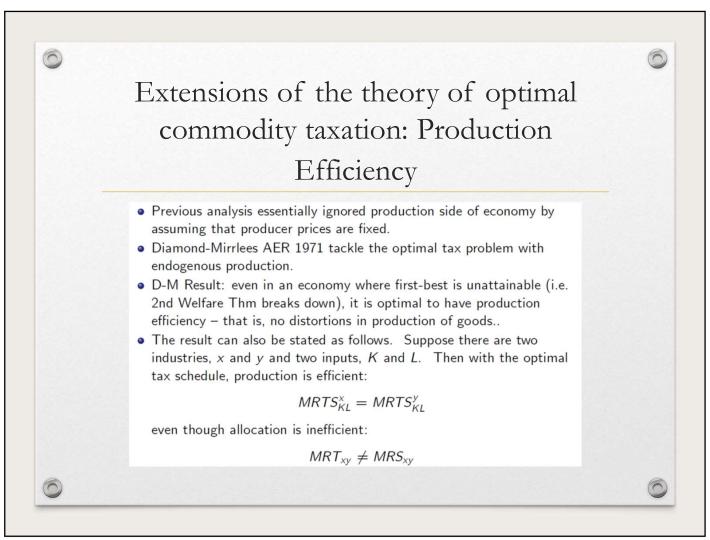
- (i) the welfare weights  $(\beta^h)$  which depend on the distributional value judgments of the government
- (ii) the marginal propensity to pay indirect taxes out of extra income  $\mathbf{t}\partial \mathbf{x}^h / \partial M^h$ .

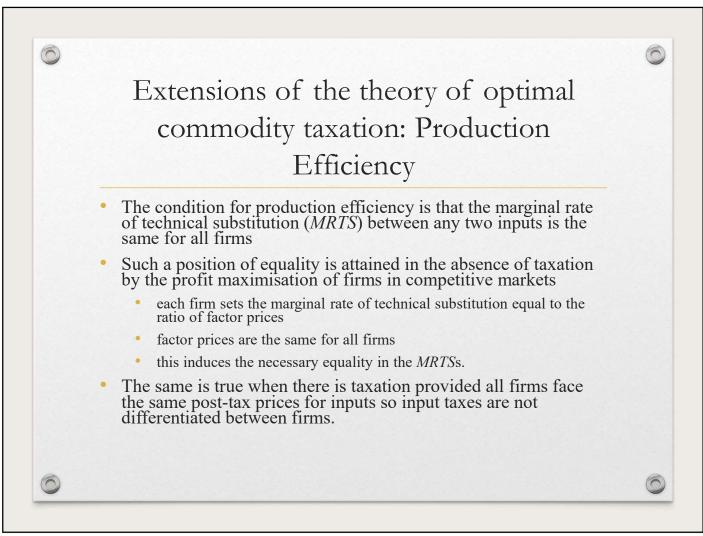


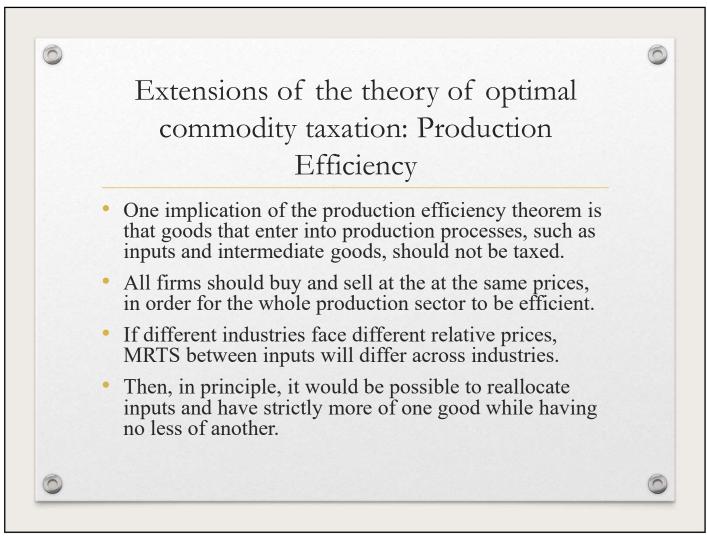


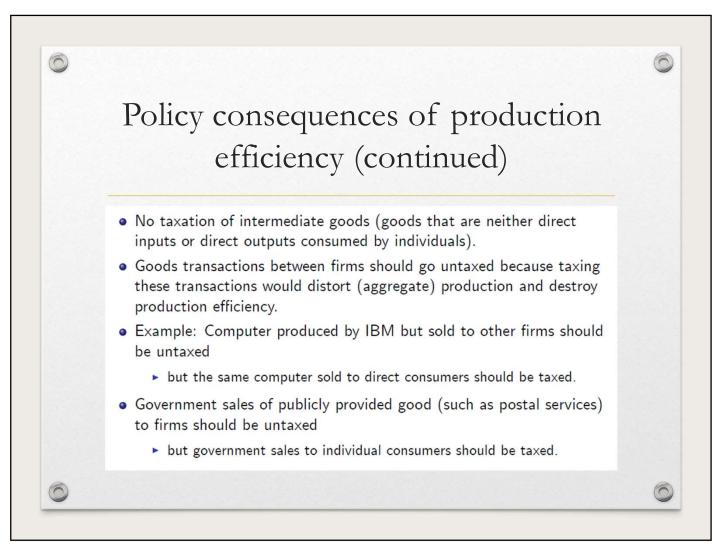










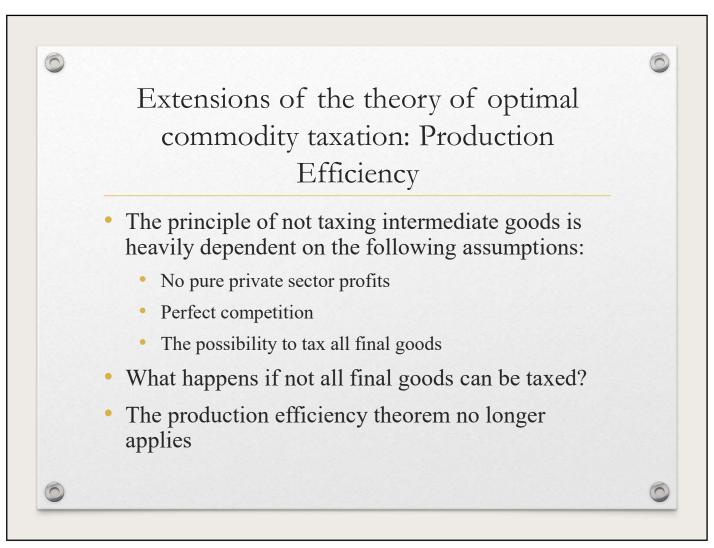


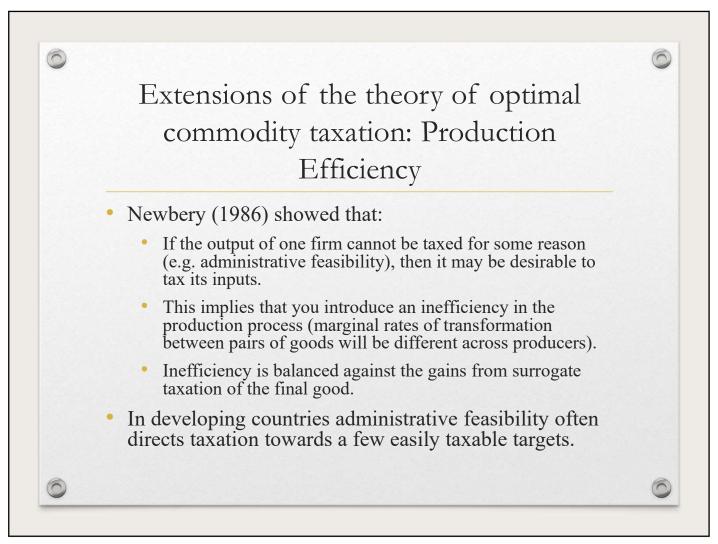


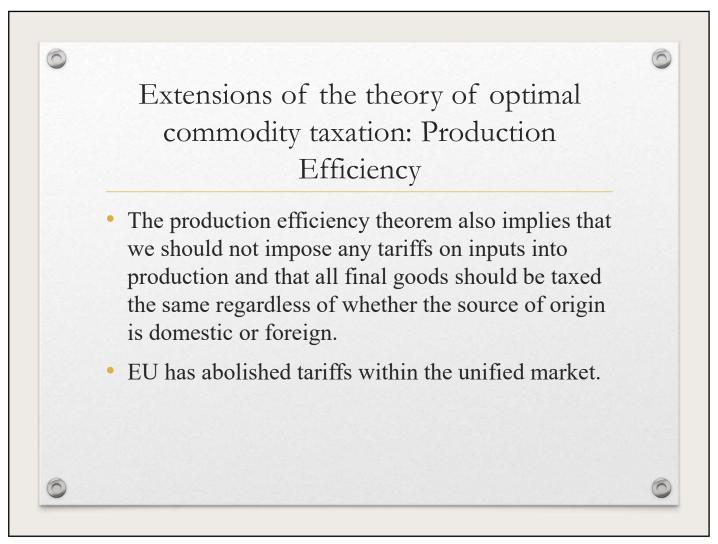


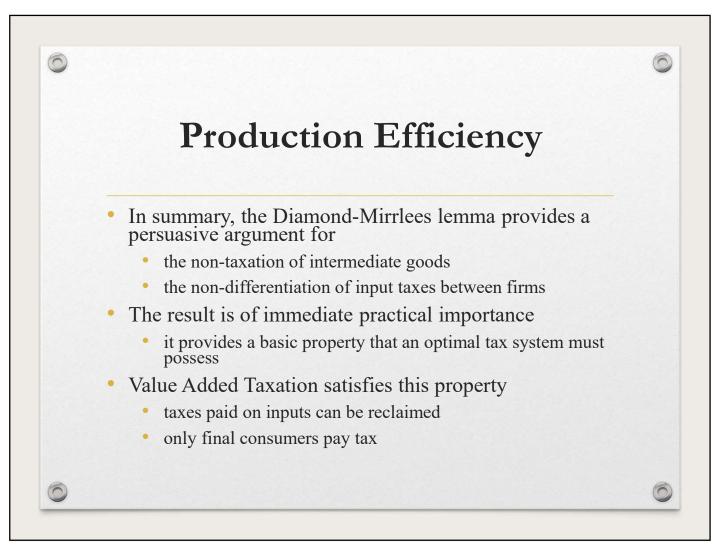
## Policy consequences of production

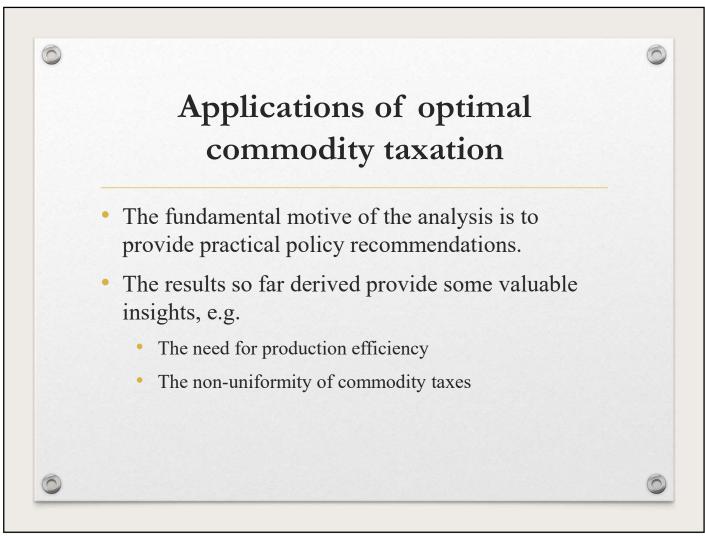
- Trade and Tariffs:
- In open economy, the production set is extended because it is possible to trade at linear prices (for a small country) with other countries.
- Diamond-Mirrlees result states that the small open economy should be on the frontier of the extended production set.
- Implies that no tariffs should be imposed on goods and inputs imported or exported by the production sector.
- Examples:
  - If IBM sells computers to other countries, that transaction should be untaxed.
  - If the oil companies buy oil from other countries, that should be untaxed.
  - ▶ If US imports cars from Japan, there should be no special tariff but should bear same commodity tax as cars made in US.

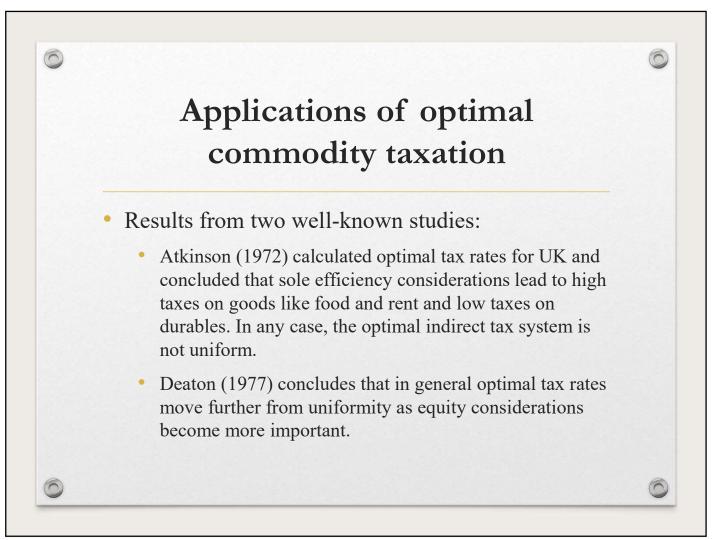


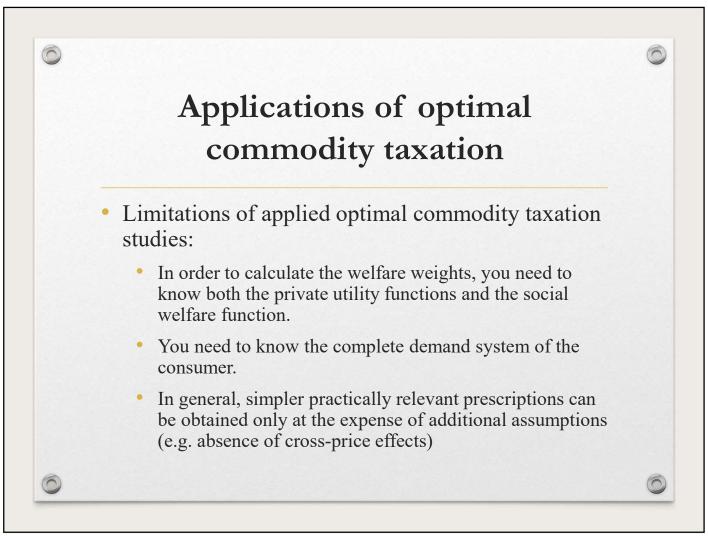


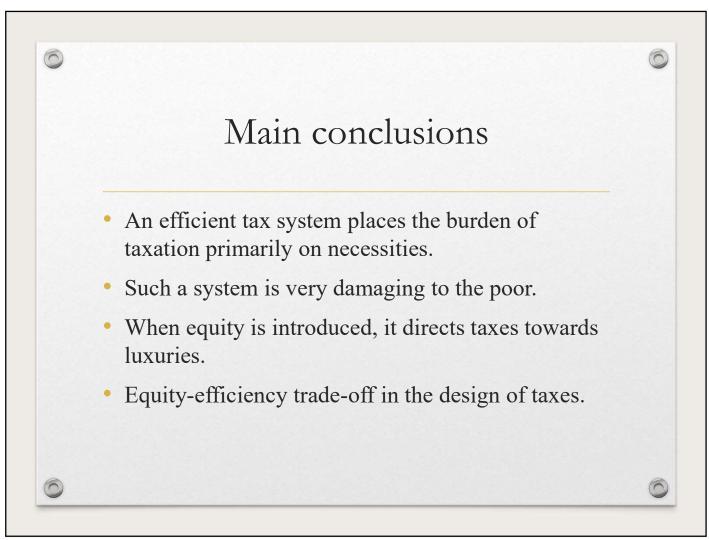


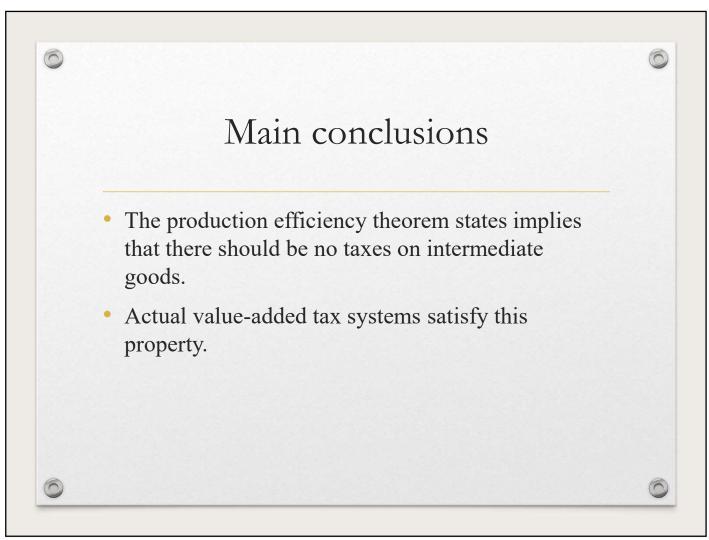


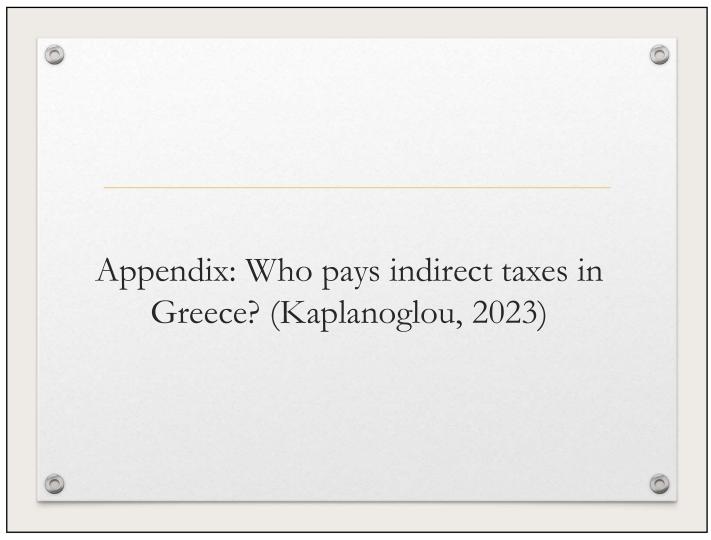


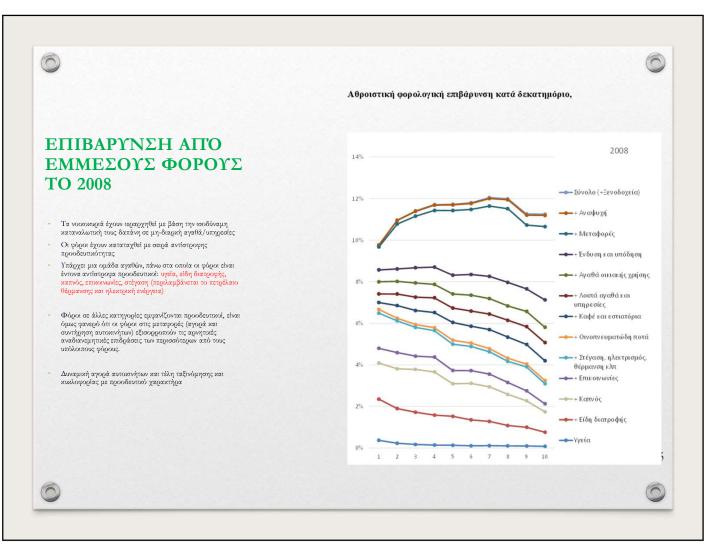


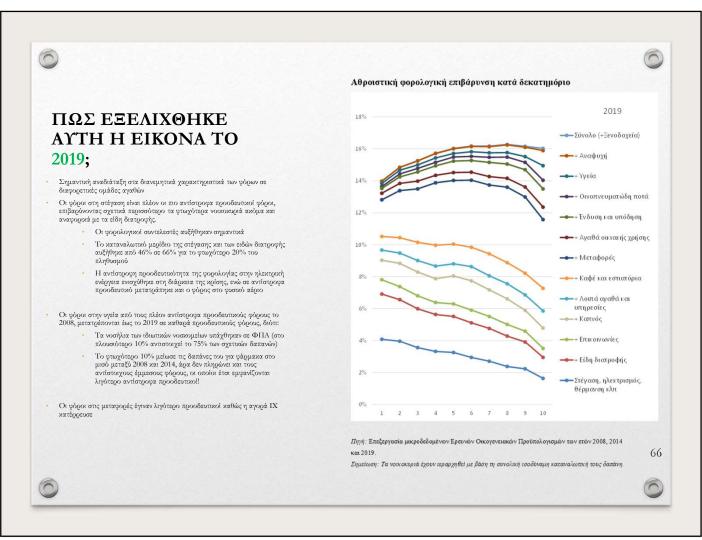
















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