

Biological information as choice and construction

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Abstract

A causal approach to biological information is outlined. There are two aspects to this approach: information as determining a choice between a set of alternatives, and information as determining the construction of a single object. The first aspect has been developed in earlier work to yield a quantitative measure of biological information that can be used to analyse biological networks. This paper explores the prospects for a measure based on the second aspect, and suggests some applications for such a measure. These two aspects are not suggested to exhaust all the facets of biological information.

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1 Introduction

Biological development is classically assumed to reflect the expression of information accumulated in the genome during evolution (Mayr 1961; Jacob 1970). Major textbooks and popular science presentation of biology rely on this picture (e.g. Alberts et al. 2013). Leading biologists are also attracted to this view (Williams 1992, p. 10; Maynard Smith and Szathmary 1995; 2000; Jablonka 2002). On closer scrutiny however, the role of information in biology seems purely instrumental: it serves either as a metaphor or as a tool for big data analyses; biology does not yet have a theory of life as an information-processing phenomenon (Sarkar 1996; Godfrey-Smith 2000). The aim of this paper is to offer some scientific substance to such a theory.

Several theoretical and philosophical approaches have interpreted living systems as information-processing systems. One tradition identifies information with meaning, interpretation, and intentionality (Barbieri 2007; Shea 2007). A second tradition, which we espouse here, identifies information with patterns of association between objects (Dretske 1981).

We start from the sense of information introduced by Crick in his sequence hypothesis and central dogma of molecular biology, which was to become massively influential in biology: ‘Information . . . means the precise determination of sequence. . .’ (Crick 1958, p. 153; see Kay 2000). Information here is causal (Šustar 2007). Crick introduced this conception in an attempt to understand how DNA and RNA carry biological specificity for the synthesis of proteins, an idea which parallels the modern contrast philosophers draw between specific causes and other necessary, background factors to obtain an effect (Woodward 2010). Griffiths and Stotz (2013, Ch. 4) have argued that Crick’s sense of information vindicates the idea that factors other than DNA are also sources of information for biomolecules, a phenomenon they

called ‘distributed specificity’. This idea needs substantiation.

We explore here this idea and develop an approach to biological information as a measurable and distinctive aspect of biological systems. Our approach has two facets, inspired from respectively Shannon’s and Kolmogorov’s approaches in information theory. On the one hand, we have a measure of the relative control exercised by several causes of the same event (Section 2). This concerns the choice between a set of alternative objects, and is blind to the information content of each object. This approach has been extensively discussed and applied elsewhere. On the other hand, we have measures of the complexity of a single cause or a single effect, independently of any particular set of alternatives (Section 3). These can measure the information inherent to a biomolecule and the quantity of information in a molecule that can be attributed to a particular source. The computability of these latter measures, however, is problematic; in practice, tentative measures ought to be used. The role of randomness in creating information is outlined (Section 4). We sketch potential developments for a Kolmogorov-inspired approach (Section 5), and argue that it is a potentially fruitful yet challenging biological research program (Section 6). The two approaches are not straightforwardly reducible to one another, and are not suggested to exhaust all aspects of biological information.

2 Causal specificity: information as choice

Recent work has defined an information-theoretic measure of the ‘specificity’ of a cause for an effect, the extent to which a cause precisely determines an effect, and applied this measure to biological problems (Griffiths et al. 2015; Calcott et al. 2017; Weber 2017; Pocheville et al. 2017). This work develops earlier, qualitative discussions of ‘causal specificity’ in philosophy (Woodward 2010) and converges with

formal work on causation in complex systems theory (see Footnote 1).

Causal specificity is measured using Shannon information theory, which conceives information as a reduction in uncertainty (Shannon 1948; Cover and Thomas 2006). Uncertainty, measured in bits, is the average number of binary (yes/no) questions that are required to determine the value of an unknown variable. A variable is said to share mutual information with another variable when it reduces our uncertainty about that variable. Mutual information measures the overlap, or redundancy, in the probability distributions of two variables: the more two variables are associated, the more each of them answers questions about the value of the other. Causal specificity can be measured by the mutual information between values of a cause variable *set by an intervention* and the value of a putative effect variable (Griffiths et al. 2015, p. 538). Formally, the causal specificity of C for E when controlling for a putative background B is given by the following formula (Pocheville et al. 2017):¹

$$I(\widehat{C}; E | \widehat{B}) = \sum_b p(\widehat{b}) \sum_c p(\widehat{c} | \widehat{b}) \sum_e p(e | \widehat{c}, \widehat{b}) \log_2 \frac{p(e | \widehat{c}, \widehat{b})}{p(e | \widehat{b})}.$$

The ‘ $\widehat{}$ ’ (hat) on a variable is an operator indicating that its value is set by an intervention, rather than observed (Pearl 2009).² This operator transforms the

¹This measure has been previously proposed in cognitive sciences (Tononi et al. 1999) and in computational sciences (Korb et al. 2009). Closely related measures have been proposed by Ay and Polani (2008) and Janzing et al. (2013). Transfer entropy is another ‘information as choice’ measure – although correlational in character, not causal (Lizier and Prokopenko 2010) – which has been applied to the study of the origins of life (Walker et al. 2017).

²As an anonymous reviewer noticed, the term $p(\widehat{c} | \widehat{b})$ implies that the intervention on C be potentially dependent on a previous intervention on B , which seems to contra-

symmetrical mutual information, representing observed association, into an asymmetric measure of causal influence, representing how much experimentally intervening on C whilst controlling for B affects E . If C is not a cause of E , then $I(\widehat{C}; E | \widehat{B}) = 0$. Reciprocally, if C is a cause of E , then there exists at least one set of background variables B (which can be empty) such that $I(\widehat{C}; E | \widehat{B}) > 0$ (Pocheville in prep.[a]).

This measure of causal specificity seems to capture one aspect of Crick's, and the above cited biologists', conception of information as 'precise determination'. It can be used to compare the causal contributions of genetic and epigenetic causes to the production of biomolecules (Griffiths et al. 2015). It can be applied to objects other than biomolecules, and is a practical tool for the analysis of biological networks (Tononi et al. 1999; Calcott et al. 2017; Pocheville in prep.[b]).

There is, however, a blindspot in Shannon information theory: it is silent about the information content of the objects themselves. For example, it makes no difference to the amount of information that DNA carries about RNA whether the DNA strands are 3 or 1416 nucleotides long. What matters is only the number of values that the variable 'DNA' can take and the probability distribution over those values. Arguably, the longer the sequences, the greater the number of possible alternatives, thus the greater the potential causal specificity of these alternatives.³ Still, in an dict the very idea of an intervention. In chosen applications however, one may decide that interventions are independent, and that $p(\widehat{c} | \widehat{b}) = p(\widehat{c})$. When the terms differ, the intervention on C can be thought of as a partial intervention, breaking all causal links pointing to C but some stemming from B .

³The Shannon entropy of a source emitting sequences of length l asymptotically tends towards the expected Kolmogorov complexity (see next section) of the sequences as $l \rightarrow \infty$. Potential causal specificity and expected Kolmogorov complexity thus go

actual case, the number of alternatives can be zero, and a very long DNA sequence can therefore have null causal specificity for its own transcript. Causal specificity represents a sense of information which enables us (or causes the system) to choose between a set of well-defined alternatives with a well-defined probability distribution. This is ‘information as choice’. If what we are interested in is the information content of a single object, another branch of information theory, Kolmogorov complexity, is more appropriate. It is to this second aspect of information that we now turn.

3 Kolmogorov meets Crick: information as construction

Kolmogorov complexity can measure the complexity of a single object (Grünwald and Vitányi 2003; Li and Vitanyi 2013). The intuitive idea is that the more complex the object, the longer its description needs to be. The Kolmogorov complexity is the length of the shortest description enabling one to reconstruct the object using a computer (or more precisely a universal Turing machine).⁴ Kolmogorov complexity also provides a measure of the amount of information in an object *about* another object. This is measured by the algorithmic mutual information: it is the amount of program length that one saves when describing one object given a description of the other object for free. Algorithmic mutual information is symmetrical.

hand in hand. We leave to future work to make this connection more explicit (see Grünwald and Vitányi 2003, p. 518; Balduzzi 2011; Li and Vitanyi 2013, p. 142).

⁴A Turing machine consists of a finite program capable of manipulating a linear list of cells (each containing a symbol, from a finite set of symbols), accessing one cell at a time. A universal Turing machine is one that can imitate any other Turing machine (Li and Vitanyi 2013, p. 22).

Obviously, the length of the shortest description will depend not only on the object at stake, but also on the language (the description method) used to write the program generating the object. However, the lengths of the shortest descriptions in two different languages will be the same up to a given translation constant, independent of the object itself. This is because the translation from one language to another can be described by a program, of which the length is fixed (which gives the constant of translation). In this sense, the Kolmogorov complexity is an objective property of the object.

A drawback of Kolmogorov complexity is that it is provably uncomputable – there is no computer program which, given any string as an input, returns its Kolmogorov complexity as an output. In itself, this is an interesting negative result: if what we are interested in is complexity in this sense, then what we want to know is simply uncomputable. In practice, one can bound the complexity of binary objects using diverse lossless compression methods (e.g. those used in the ZIP file format). Indeed, the compressed object is a (hopefully shorter) description enabling one, together with a decompression program, to reconstruct the initial object. The length of description is then the length of the compressed file plus a constant, the length of the decompression program. This measurement is tentative, not definitive, as other, potentially unknown compression methods might compress the object more. For the sake of the argument, we assume for the moment that we are given a reasonable compression method.

Kolmogorov complexity can be used to explore what Crick meant when he described the determination of proteins by nucleic acids as the “detailed residue-by-residue transfer of sequential information” (Crick 1970, p. 561), where nucleotides would form a quaternary alphabet and amino-acids a vigesimal one. Two kinds of questions can be addressed: about how much information there is in a given

biological object, and, closer to Crick's thinking, about how much information in an object comes from another.⁵

The complexity of a strand of DNA, for instance, can be approached by measuring the length of the compressed sequence. Telomeres provide an interesting limit-case. They are nucleotide sequences at the end of chromosomes, consisting of a repetitive pattern (e.g. TTAGGG in humans, and many other species). Telomeres are elongated by an enzyme, called telomerase, which embeds an RNA-sequence as a template (Hiyama et al. 2009). It is not difficult to come up with a program describing a given telomeric sequence in a compact way. Whatever the length of a telomere, it can be described by a template for the repeated pattern and the number of repeats (Figure 1, Algorithm 1). A naive observer would surely think that telomeres do not contain much information, and in particular not much *sequential* information. The intuition here coincides with the low Kolmogorov complexity of these sequences.

The situation looks quite different for coding sequences. There does not seem to be, at first sight, as easy a way to compress these sequences as we did with telomeres, and their Kolmogorov complexity is probably substantially higher: a program to reconstruct a coding sequence may have to spell it out explicitly – or at least to spell out significant aspects of the sequence (Fig. 1, Alg. 2). This lower compressibility coincides with the intuition that coding sequences carry sequential information – and even that it is their function to carry sequential information. However, coding sequences do not carry a maximal amount of sequential information: as an anonymous reviewer noticed, coding sequences are structured, and are thus expected

⁵On the algorithmic approach in biology, see e.g. Yockey (2005, p. 170) and especially Chaitin (1979; 2012), and the discussion by Artmann (2008, pp. 32-37). We lack space to review the independent convergences and divergences of the here proposed account.

to be compressible to some extent – as are non-coding, so-called ‘junk’ DNA-sequences containing a significant number of repetitive elements and duplications.⁶ Note that the intrinsic amount of information in a sequence is independent of whether the sequence is inserted in a region which will actually undergo transcription. Arguably, even a coding sequence carries no information *about* any transcript if it is not transcribed, but it nevertheless carries sequential information *tout court*.

We now turn to the second question, asking how much information there is in an object *about* another object. For the sake of the argument, we suppose that the world is as Crick supposed in 1958: the accuracy of information transfers is high, which we idealize by assuming that transcription (of DNA into RNA) and translation (of RNA into polypeptides) are error-free, deterministic processes. We ignore splicing and other post-transcriptional processes, which will be treated elsewhere. As described above, one can estimate the amount of information in DNA about RNA by their algorithmic mutual information, that is: $I(DNA : RNA) = K(RNA) - K(RNA | DNA^*)$.⁷ The shared information between DNA and RNA is substantial: the transcription process is all about replacing the nucleotides by their complementary ones, with the proviso that As in the coding DNA-sequence are complementary to Us (not Ts) in the RNA-sequence. To see this sharing of information, compare the lengths of an algorithm spelling out the RNA explicitly (similar to Alg. 2) and one treating transcription generically (Fig. 1, Alg. 3). The difference in length would increase with sequence length. This corresponds to the fact that sequential information is transferred from DNA to RNA through transcription. If transcription is errorless, the sequential information in RNA which does not come from DNA, measured by the

⁶Whether the compressibility of sequences is an inevitable aspect of their biological function is precisely a question we wish to address in the long term.

⁷Where DNA^* is the shortest program generating DNA .

remainder complexity $K(RNA | DNA^*)$, is a constant, independent of the sequence. Algorithmic mutual information between biological sequences has been used in the past decade with various aims, such as the building of phylogenetic trees according to the amount of information needed to transform one DNA sequence into another (e.g. Chen et al. 2000; Li et al. 2001; Chen et al. 2002; Vinga 2013, for a review).

Since the ‘true’ Kolmogorov complexity is uncomputable, an algorithmic approach relies on a bet – that the language of description and compression methods capture interesting and relevant aspects of the object at stake. This is not to say that the approach is necessarily entirely arbitrary: once these methods are agreed upon, researchers can agree on the measures obtained for finite sequences. If a particular language gives particularly interesting results (e.g. saving biological appearances, leading to new questions, predictions and generalizations), then this language becomes a theoretical entity worth discussing in its own rights. In the remainder of the paper, we outline what we deem desirable features for such a language, and substantially develop the algorithmic approach to take into account the fact that biological systems are not, strictly speaking, deterministic, universal Turing machines. What we aim at is not an application of conventional algorithmic information theory to biology, but a specifically biological approach to information inspired by the Kolmogorov branch of information theory.

<hr/> Algorithm 1: Function synthesizing a telomeric sequence of a defined length. <hr/> Function <i>SynthesizeTelomere</i> (<i>n</i> , <i>RNA-template</i>) input : <i>n</i> : number of iterations, <i>RNA-template</i> : ‘CCCAAUCCC’ output : a given telomere for <i>i</i> ← 1 to <i>n</i> do apply <i>telomerase</i> using <i>RNA-template</i> end end <hr/>	<hr/> Algorithm 2: Function synthesizing a given (bit of) coding DNA from scratch. <hr/> Function <i>SynthesizeCodingSequence</i> input : none output : a given coding sequence synthesize ‘...GCAGTAGAATT CCGAGCAAACCTGAACGAGCA GTAGAA...’ end <hr/>
<hr/> Algorithm 3: Function synthesizing a RNA given a DNA as an input. <hr/> Function <i>SynthesizeRNA</i> (<i>DNA</i>) input : a given DNA output : a given RNA while in <i>DNA</i> do transcribe <i>nucleotide</i> move forward <i>one nucleotide</i> end end <hr/>	<hr/> Algorithm 4: Function spelling out transcription in (some) details. <hr/> Function <i>Transcribe</i> (<i>nucleotide</i>) input : nucleotide output : corresponding nucleotide if <i>A</i> then return <i>U</i> else if <i>C</i> then return <i>G</i> else if <i>G</i> then return <i>C</i> else if <i>T</i> then return <i>A</i> end <hr/>

Figure 1: Four algorithms illustrating an algorithmic approach to biological functioning.

4 Randomness as the source of information

We made several idealising assumptions in the previous sections. Let us now relax the assumption that cellular processes are deterministic. Our argument here will remain theoretical: we lack room to take sides on whether, and how, randomness is actually realized in biology.⁸

⁸Doing so properly would require developing an account of measurement in biology, as those developed for deterministic chaos and quantum indeterminacy. In deterministic chaos, any finite measurement of the initial condition will leave aside information (the amount of which is infinite) which will manifest itself after a certain time in the

Random events, by definition, cannot be determined in advance by an algorithm. This means that randomness in the generation of a sequence creates information *de novo*. In biological terms, this means that any random point mutation, any error of transcription, etc., if they are genuinely random, can create information in the Kolmogorov sense. As we have seen in the previous section, this also means that randomly generated sequences contain more information than highly structured sequences. From an algorithmic point of view, randomness is, ultimately, the only way to create information.

This information need not always be functional, that is, of any use to the cell. That it may *sometimes* be so, however, is a reasonable assumption. There are several biological examples suggesting that randomness plays a key role in biological functioning (Kupiec 1983; Heams 2014). Gene shuffling in the immune system of jawed vertebrates provides one such example regarding biological sequences. It enables a great variety of antibodies to be produced, orders of magnitude more numerous than the genes producing them, increasing the chance of matching potentially threatening antigens (Cooper and Alder 2006).

This tension between information and function is why it is crucial to distinguish them. One might be interested in how information flows in biological systems without committing oneself to a particular account of biological function. More importantly, if one is interested in whether and how information leads to function, a concept of biological information as necessarily biologically functional will beg the question.

system (Montévil 2018, § 2.1, 2.3). Quantum indeterminism represents another entry to a physicalist view of the appearance of information (Stamos 2001, and the responses).

5 A language for the cell

Kolmogorov complexity allowed us to flesh out the idea of information as construction. Now we need to kick that ladder away and ask what information as construction actually looks like in living systems. We suggest that it ought to be measured using a particular programming language: the language of the cell itself, in which available programming functions mimic actual operations by which molecules are produced. It goes without saying that what we evoke here is not the ‘true’ language, but a model of a language of the cell.

The idea of a language of the cell takes us away from treating cells as universal Turing machines and from the genuine Kolmogorov complexity K , to consider a more biological algorithmic complexity, the Kolmogorov complexity in the chosen biological language (hereafter denoted K_B). For instance, algorithmic mutual information is symmetric – there is as much information in DNA about RNA as there is in RNA about DNA, i.e. $I(RNA : DNA) = I(DNA : RNA)$. But not all operations are possible in a cell. A central feature of molecular biology is that flows of information are asymmetrical. Crick’s ‘central dogma’ (still widely held today) states which flows of information between biomolecules are possible and which are not. If no reverse-transcriptase is present, for instance, no information can flow from RNA to DNA. In ‘biologically’ algorithmic terms, this means that a biological program aiming at reconstructing a DNA-sequence being given an RNA-sequence as an input would fare no better than a program being given no input, and we would obtain $K_B(DNA | RNA^*) = K_B(DNA)$. This means that we would get, as for a biological analog of algorithmic mutual information, $I_B(RNA \rightarrow DNA) = K_B(DNA) - K_B(DNA | RNA^*) = 0$. (The subscript ‘ B ’ again denotes that the measure is defined using the chosen biological language, and the

arrow now reflects that it can be asymmetric.⁹) The reciprocal, as we have seen above, is very different: when DNA is transcribed into RNA, $K_B(RNA | DNA^*) = C$, where C is a constant not depending on the sequences. Assuming, for the sake of presentation, that $K_B(RNA) = K_B(DNA)$, we would obtain $I_B(DNA \rightarrow RNA) = K_B(RNA) - K_B(RNA | DNA^*) = K_B(DNA) - C$. Thus, contrary to its genuine counterpart, biological algorithmic mutual information would not be expected to be always symmetrical, reflecting the directionality of possible information flows.

In the same vein, not all sequences can be produced by a given cell. In algorithmic information theory, a universal Turing machine can emulate any other Turing machine, which means that there is no sequence that a particular machine can produce that a universal machine cannot produce. By contrast, if the cell lacks a programming function, for instance, if it lacks a nucleic acid template, or if some nucleotides do not belong to its alphabet, then some sequences may be impossible to produce. In this case, the information needed to produce an impossible sequence is ill-defined, in other words, the amount of information needed to produce the sequence is indefinite. Even on an evolutionary time-scale, the amount of information needed to acquire the programming function (if it is acquired) and produce the previously-impossible sequence could be orders of magnitude greater than the length of the sequence.

Granted that some operations are impossible, how are we to describe the set of primitive programming functions which, by contrast, are possible?

As we have seen above, the complexity of an object depends on the language used to describe it. An example will flesh out this idea. Assume, say, that ‘Transcribe’ is

⁹We follow the notation used for one asymmetrical, causal version of Shannon mutual information (Ay and Polani 2008).

given for free by the language, and that the description of the function is short: say, just a few letters. Contrast this with a DNA sequence of several kilobases. This DNA sequence appears much more informational than the function ‘Transcribe’.¹⁰ Now, imagine that ‘Transcribe’ is not given for free by the language, but that one has to write a program for this function, using other, more primitive, available functions. We exemplify such a program in Alg. 4 (Fig. 1) – it could be made much longer by describing explicitly the dynamics of chemical bonds in a binary manner (assuming for the sake of the argument that this would be feasible). Conversely, the description of a long DNA-sequence can be very short. For instance, nominal genes are usually described, not by their full sequence, but by a nickname like ‘p53’. This nickname is enough, on most occasions, for biologists to communicate about the processes at stake. A language can lack the function ‘Transcribe’ but have a built-in function ‘P53’ dedicated to returning the full sequence of the gene. In such a language, descriptions of transcription would be complex (informational) and that of DNA simple. Thus, one needs to be cautious about the language of description before assigning any particular object a privileged informational role – much in the same way as one needs to be cautious about specifying the probability distributions when using Shannon information theory.

We propose that the primitive functions should be those which enable us to understand the processes of interest. Assume, for instance, that our interest lies in understanding the flows of sequential information between biological polymers. Then assuming that ‘Transcribe’ and ‘Translate’ are given as primitive functions is fine: if they are errorless, they are not difference-makers as regards the final sequences of the

¹⁰Many biologists and some philosophers routinely ascribe to DNA a privileged informational role. One way to reconstruct this idea is to consider that they implicitly assume such a language.

products (an assumption that we made in Alg. 3). Generally speaking, it makes sense to consider as primitives those operations which are not difference-makers as regards the outputs of interest, and as inputs those very difference-makers: the genericity for functions, and the specificity for inputs. Incidentally, it is good algorithmic practice to write functions for generic operations and give them specific variables as inputs. This is not unlike causal specificity: once the generic functional relationships in the causal model are set, information flows from difference-makers.

6 Payoff of the approach

The algorithmic approach sketched above may promote research on biological systems, although not without significant challenges.

Even the best current specifically designed compression algorithm may overestimate biological complexity. This is because the algorithm may not have compressed the object sufficiently. On the positive side, compression algorithms may actually tend to parallel the biological processes that have produced the sequences at stake. For instance, if DNA translocation is frequent, then an algorithm that pays due attention to translocation should be more likely to compress a DNA-sequence. Conversely, considering that most strings are random in the algorithmic sense, it is highly unlikely that a series of refined algorithms will converge, if they do converge, towards something other than the processes involved in producing the sequences. It is highly unlikely that the cell will, by chance, produce a string which is compressible by other means than some of its own means of production (or the corresponding models of these means). In other words, improving these algorithms may yield a better grasp of functions which are in fact available in the language of the cell.

Just as an algorithm may overestimate complexity, however, it can also *underestimate* biological complexity. Because cells are not universal Turing machines, a biological sequence may be more complex than its algorithmic counterpart. For instance, a cell may need a complex process to resist random perturbations when duplicating a sequence, while a universal Turing machine, being deterministic, would not. Similarly, a short sequence may require a complex machinery or a complex evolutionary history to produce it. Just as biological complexity can shortcut algorithmic complexity (when a cell generates randomness), it can also exceed it.

7 Conclusion

This paper aimed to give substance to the idea of biological information – an idea which has grounded significant aspects of informal biological thought for the past fifty years. Crick’s seminal use, in molecular biology, of the term ‘information’, meaning the precise determination of sequence, is grounded on causation, not meaning or representation. We inflected this idea in two ways, corresponding to two aspects of information theory: the precise determination of a single output from a set of alternatives (‘information as choice’), and the precise determination of the sequence of a single output (‘information as construction’). These two aspects can be traced back to Crick, whose idea of information as construction – to rephrase in our terms – was an attempt to provide an explanation of information as choice, in the sense of biological specificity (Crick 1958; Crick 1970). This suggests that Griffiths’ and Stotz’s (2013) idea of distributed specificity is theoretically richer than initially envisioned.

Information as choice is captured by causal specificity, proposed elsewhere to be measured by the Shannon mutual information between values of a cause set by an

intervention and observations of the effect. This measure can be applied to causal graphs, such as those representing gene regulatory or animal signalling networks, and has numerous potential applications in biology.

Information as construction is captured by the Kolmogorov complexity of a sequence and the algorithmic mutual information between two sequences. These measures capture the intuition that there is something in common between a program generating a sequence and the biological processes of transcription and translation. We insisted, however, that there is more to biology than discrete, deterministic computing: randomness plays a central role in biological functioning. A similar point could be made regarding the non-discrete nature of biological phenomena. From the point of view of Kolmogorov complexity, randomness creates information. Such information is not necessarily functional, and distinguishing between information and function is a necessary step towards better understanding how information can lead to function.

We proposed that biological algorithmic complexity ought to be measured using a biologically relevant programming language – the language in which the cell performs its own operations. In such a language, some operations, such as reverse-translation, will be impossible. This means that the biological complexity of a sequence can far exceed its own length – making it very different from non-biological algorithmic complexity. In planned future work, we will take up the challenge of fleshing out the ‘language of the cell’, and articulating the choice and construction aspects of biological information.

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Algorithm 1: Function synthesizing a telomeric sequence of a defined length.

Function *SynthesizeTelomere*(n ,
RNA-template)
 input : n : number of iterations,
 RNA-template:
 ‘CCCAAUCCC’
 output : a given telomere
 for $i \leftarrow 1$ to n do
 | **apply** *telomerase* using
 | *RNA-template*
 end
end

Algorithm 3: Function synthesizing a RNA given a DNA as an input.

Function *SynthesizeRNA*(*DNA*)
 input : a given DNA
 output : a given RNA
 while in *DNA* do
 | **transcribe** *nucleotide*
 | **move forward** *one nucleotide*
 end
end

Algorithm 2: Function synthesizing a given (bit of) coding DNA from scratch.

Function *SynthesizeCodingSequence*
 input : none
 output : a given coding sequence
synthesize ‘...GCAGTAGAATT
 CCGAGCAACTGAACGAGCA
 GTAGAA...’
end

Algorithm 4: Function spelling out transcription in (some) details.

Function *Transcribe*(*nucleotide*)
 input : nucleotide
 output : corresponding nucleotide
 if *A* then return *U*
 else if *C* then return *G*
 else if *G* then return *C*
 else if *T* then return *A*
end
