

Fig. 12-3 The radial functions  $R(r)$  for hydrogen.  
 [Note: The radius is measured here in angstroms rather than in Bohr radii.] The units of  $R$  are  $10^{12} \text{ cm}^{-3/2}$

ΠΙΝΑΚΑΣ 9.3. Οι ακτινικές συναρτήσεις  $R_{n\ell}$  μέχρι  $n = 3$

	$\ell = 0$	$\ell = 1$	$\ell = 2$
$n = 1$	$R_{10} = 2e^{-r}$		
$n = 2$	$R_{20} = \frac{1}{\sqrt{2}} \left(1 - \frac{r}{2}\right) e^{-r/2}$	$R_{21} = \frac{r}{2\sqrt{6}} e^{-r/2}$	
$n = 3$	$R_{30} = \frac{2}{3\sqrt{3}} \left(1 - \frac{2r}{3} + \frac{2r^2}{27}\right) e^{-r/3}$	$R_{31} = \frac{8r}{27\sqrt{6}} \left(1 - \frac{r}{6}\right) e^{-r/3}$	$R_{32} = \frac{4r^2}{81\sqrt{30}} e^{-r/3}$

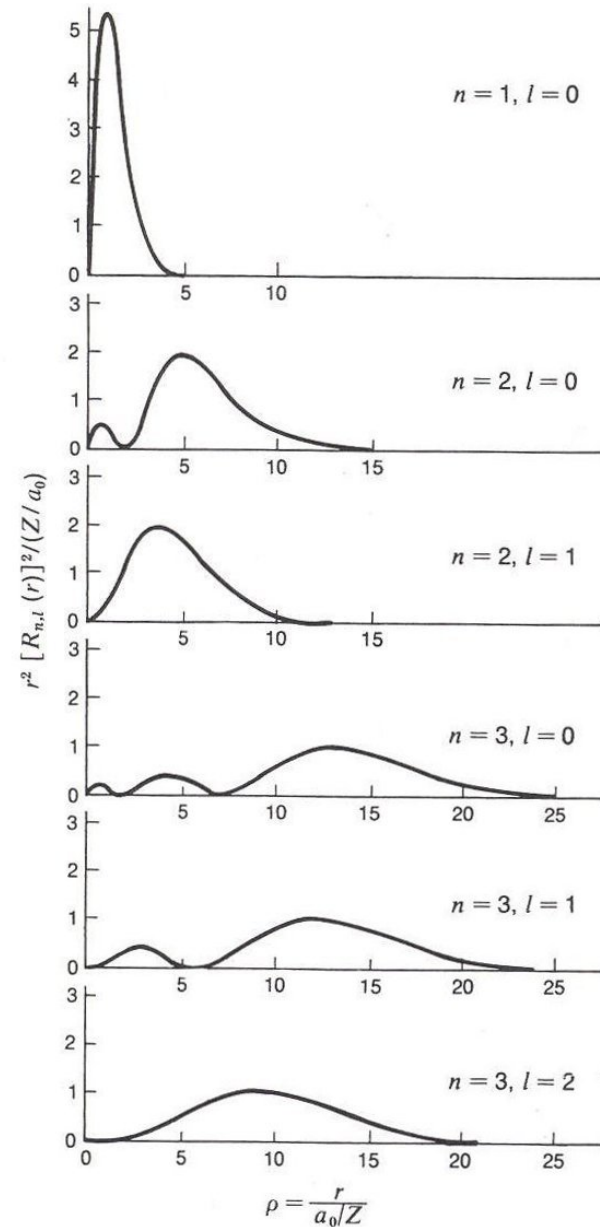
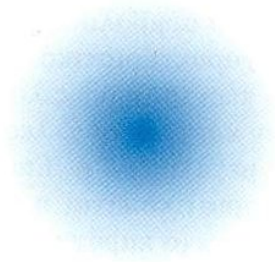
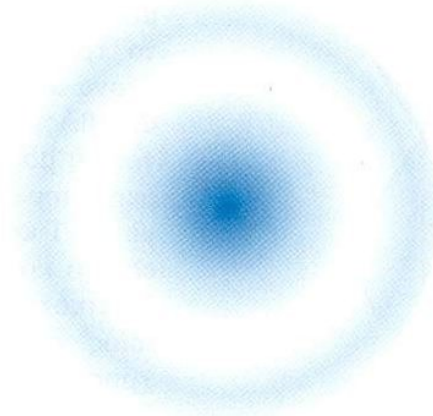


Fig. 12-5 Radial probability distribution for several states of hydrogen.  
 [Note: the horizontal axis is in Bohr radii for  $Z = 1$ .]



Τροχιακό 1s

$$\left( \psi_{1s} = \frac{1}{\sqrt{\pi}} e^{-r} \right)$$



Τροχιακό 2s

$$\left( \psi_{2s} = \frac{1}{2\sqrt{2\pi}} \left( 1 - \frac{r}{2} \right) e^{-r/2} \right)$$

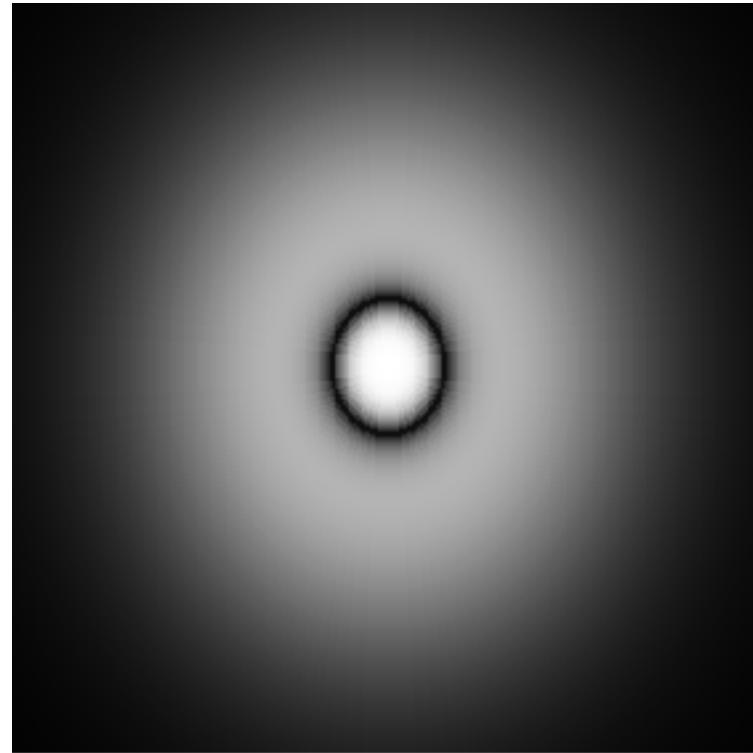


n= 1

l= 0

m= 0

H 1S

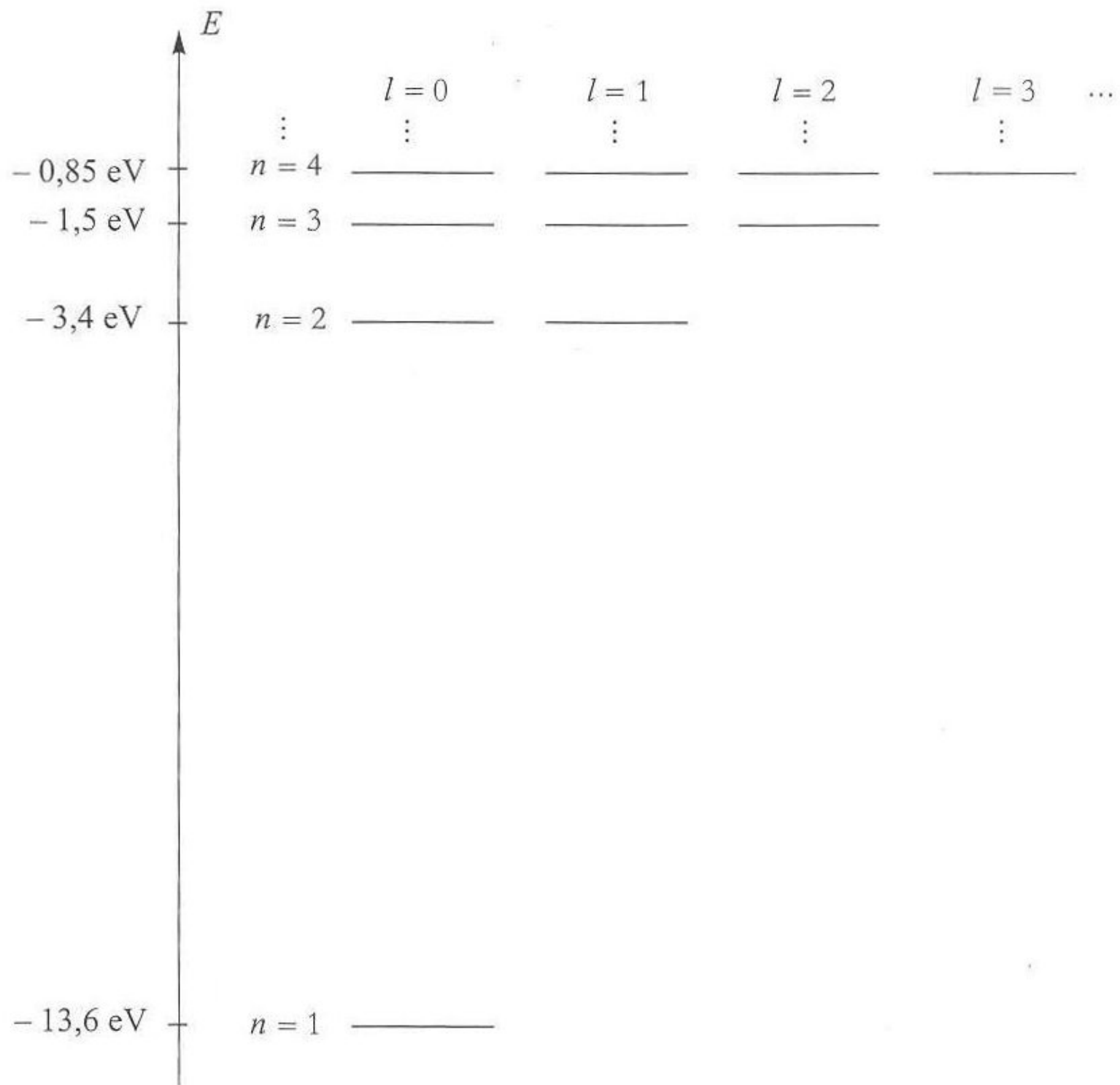


n= 2

l= 0

m= 0

H 2S



Group Period	→ 1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1	1 H																	2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
6	55 Cs	56 Ba	57 La *	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
7	87 Fr	88 Ra	89 Ac *	104 Rf *	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
			* 58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu		
			* 90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr		

$$1S \quad \varphi_{100}(r, \theta, \phi) = \frac{2}{(a_0)^{\frac{3}{2}}} e^{-r/a_0} \Upsilon_0^0(\theta, \phi)$$

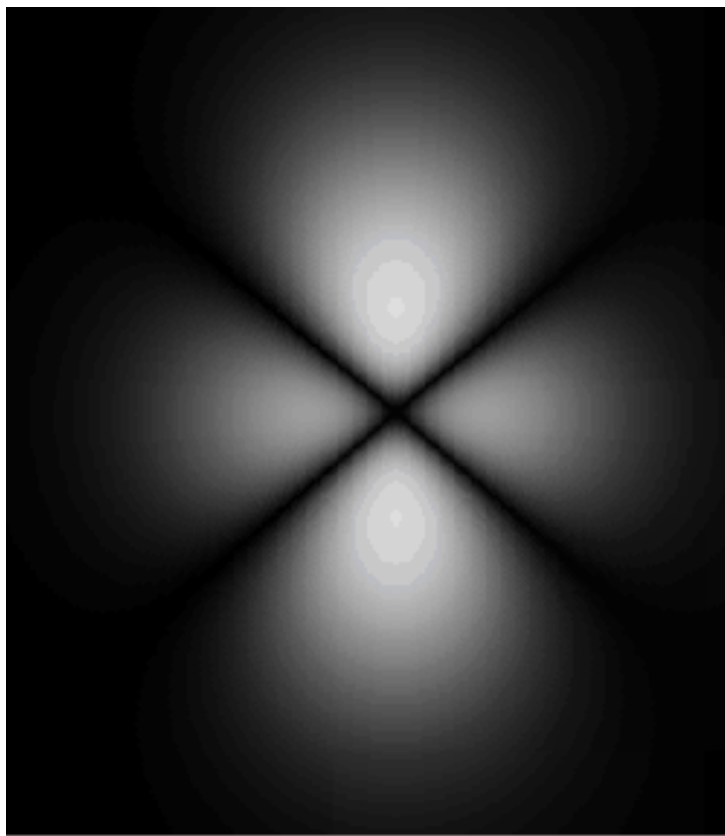
$$2S \quad \varphi_{200}(r, \theta, \phi) = \frac{2}{(a_0)^{\frac{3}{2}}} \left(1 - \frac{r}{2a_0}\right) e^{-r/2a_0} \Upsilon_0^0(\theta, \phi)$$

$$2P \quad \left. \begin{array}{l} \varphi_{211}(r, \theta, \phi) \\ \varphi_{210}(r, \theta, \phi) \\ \varphi_{21-1}(r, \theta, \phi) \end{array} \right\} = \frac{1}{\sqrt{3}(2a_0)^{\frac{3}{2}}} \frac{r}{a_0} e^{-r/2a_0} \begin{cases} \Upsilon_1^1(\theta, \phi) \\ \Upsilon_1^0(\theta, \phi) \\ \Upsilon_1^{-1}(\theta, \phi) \end{cases}$$

$$3S \quad \varphi_{300}(r, \theta, \phi) = \frac{2}{3(3a_0)^{\frac{3}{2}}} \left\{ 3 - \frac{2r}{a_0} + 2 \left( \frac{r}{3a_0} \right)^2 \right\} e^{-r/3a_0} \Upsilon_0^0(\theta, \phi)$$

$$3P \quad \left. \begin{array}{l} \varphi_{311}(r, \theta, \phi) \\ \varphi_{310}(r, \theta, \phi) \\ \varphi_{31-1}(r, \theta, \phi) \end{array} \right\} = \frac{4\sqrt{2}}{9(3a_0)^{\frac{3}{2}}} \frac{r}{a_0} \left(1 - \frac{r}{6a_0}\right) e^{-r/3a_0} \begin{cases} \Upsilon_1^1(\theta, \phi) \\ \Upsilon_1^0(\theta, \phi) \\ \Upsilon_1^{-1}(\theta, \phi) \end{cases}$$

$$3D \quad \left. \begin{array}{l} \varphi_{322}(r, \theta, \phi) \\ \varphi_{321}(r, \theta, \phi) \\ \varphi_{320}(r, \theta, \phi) \\ \varphi_{32-1}(r, \theta, \phi) \\ \varphi_{32-2}(r, \theta, \phi) \end{array} \right\} = \frac{2\sqrt{2}}{27\sqrt{5}(3a_0)^{\frac{3}{2}}} \left( \frac{r}{a_0} \right)^2 e^{-r/3a_0} \begin{cases} \Upsilon_2^2(\theta, \phi) \\ \Upsilon_2^1(\theta, \phi) \\ \Upsilon_2^0(\theta, \phi) \\ \Upsilon_2^{-1}(\theta, \phi) \\ \Upsilon_2^{-2}(\theta, \phi) \end{cases}$$

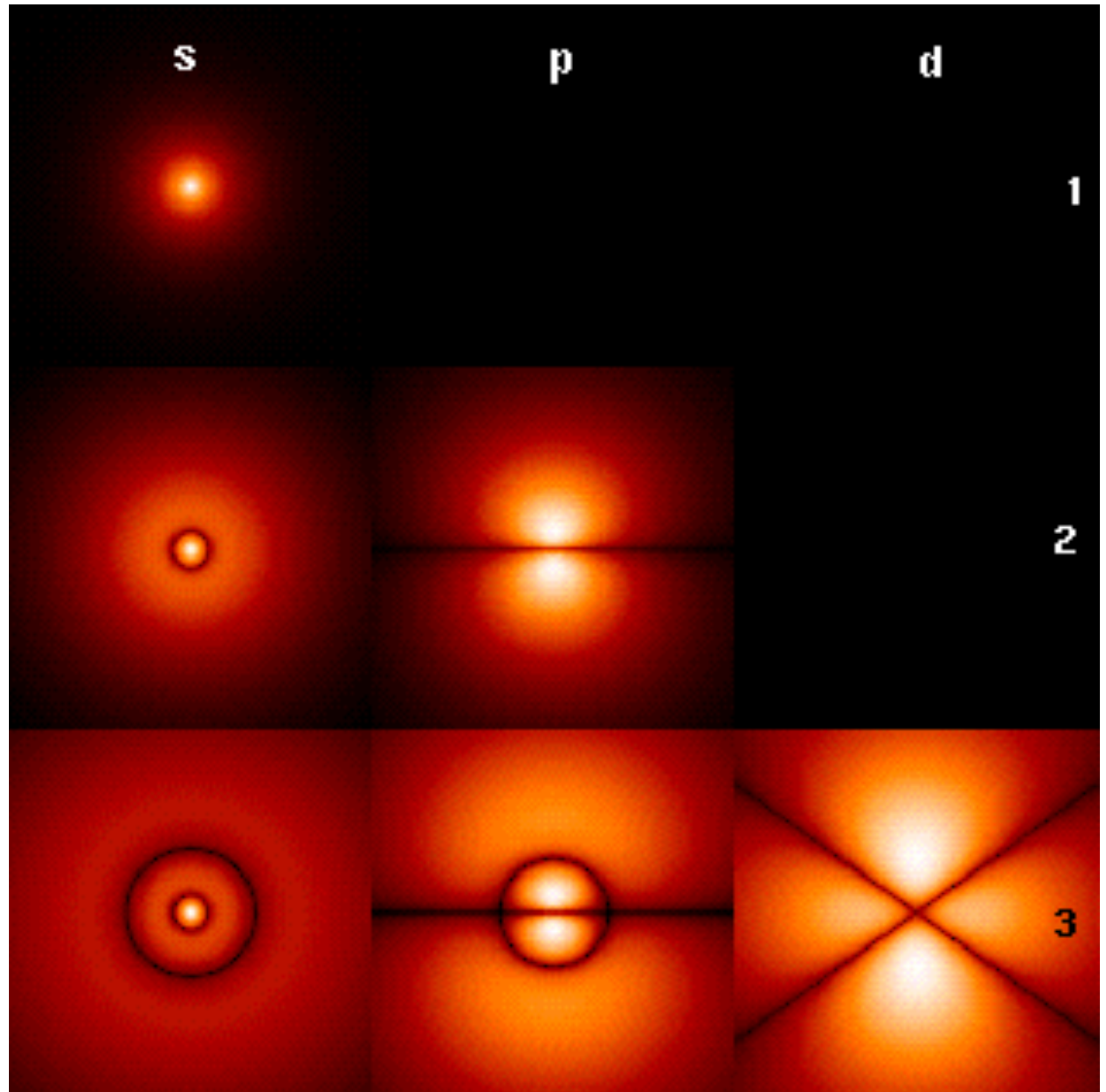


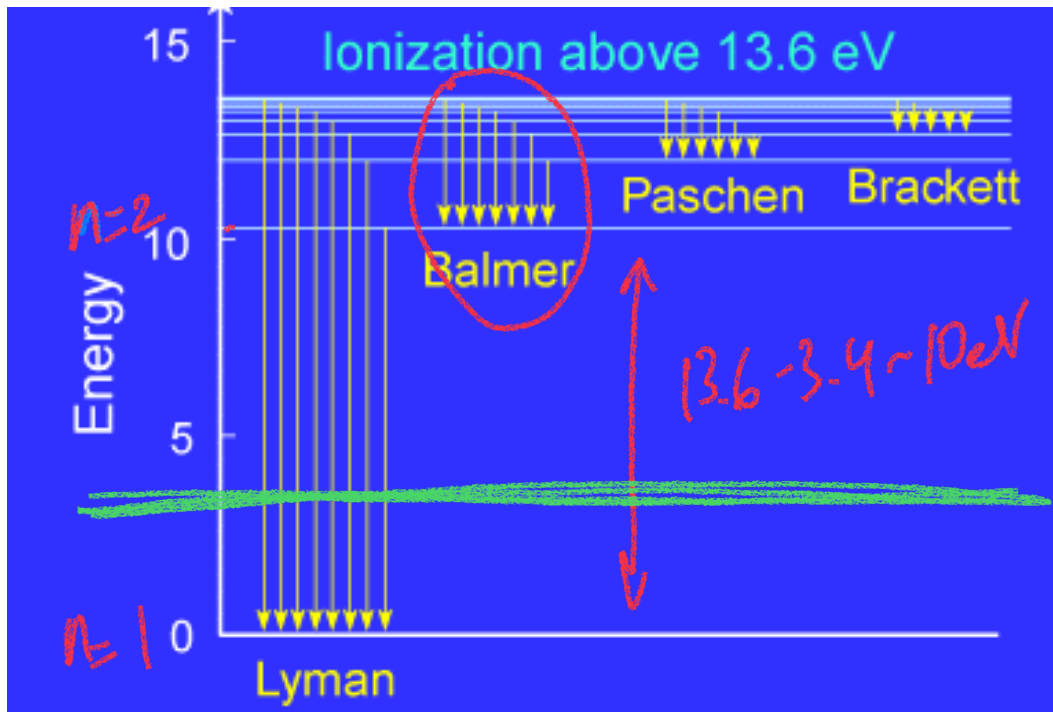
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l= 2

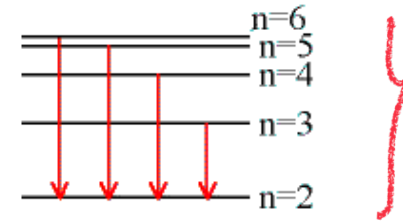
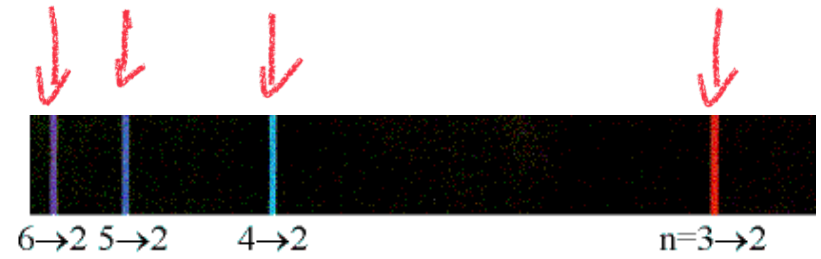
m= 0

H 3D



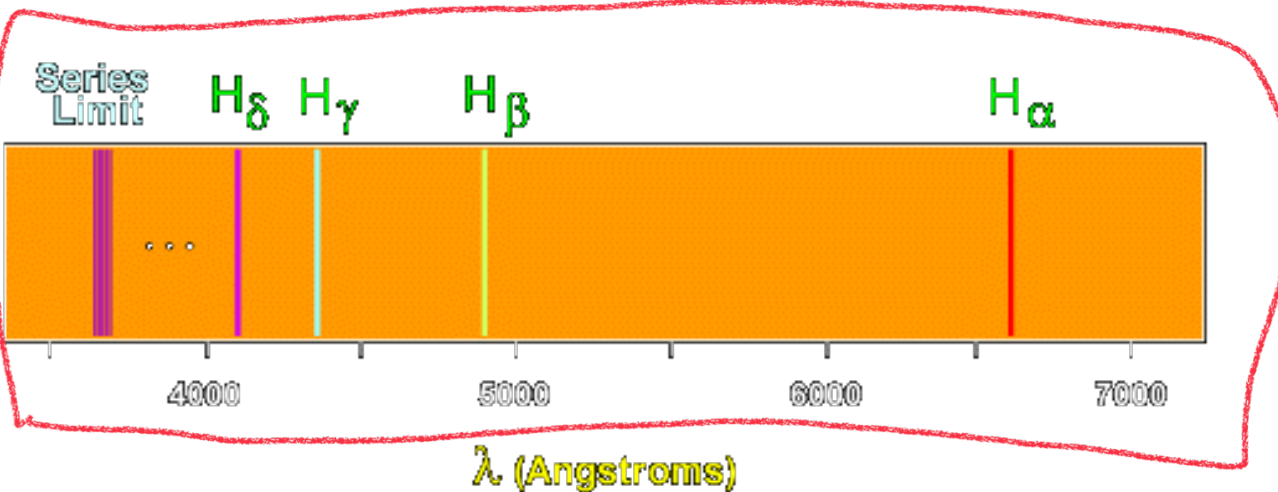


Γραμμές Υδρογόνου



—————  $n=1$  (Ground State)

$$i\hbar \frac{\partial \psi}{\partial t} = \hat{H} \psi$$



Γραμμές Balmer